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# *Quantum Cryptography*

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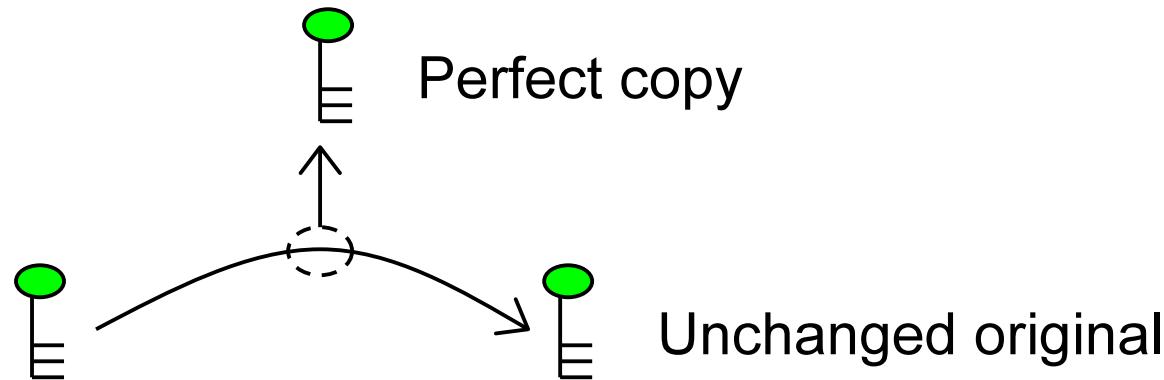
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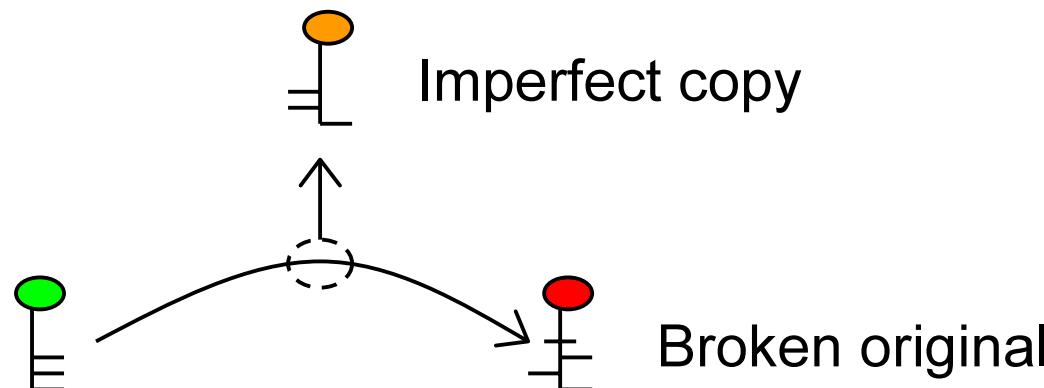


# Classical vs. quantum information

- **Classical information**

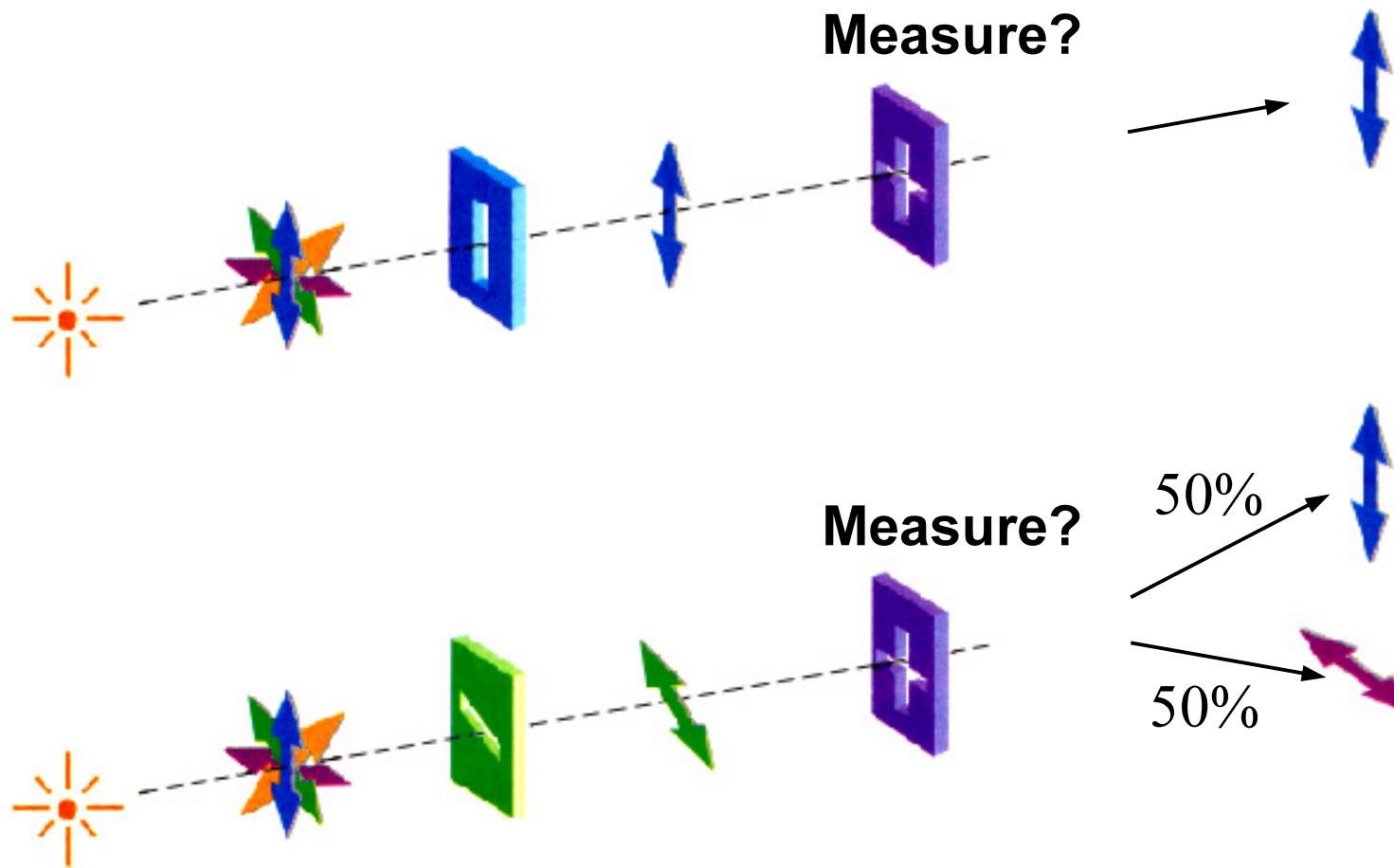


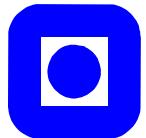
- **Quantum information**





# Qubit: polarization state of a single photon





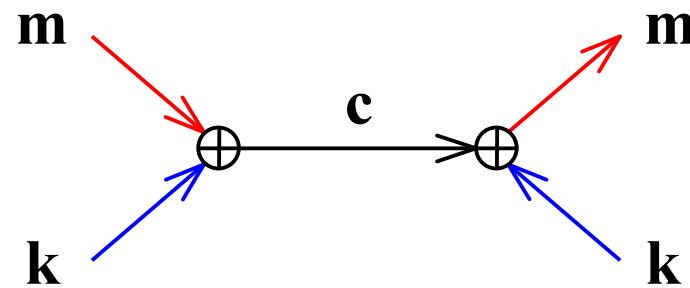
# What is the problem with classical cryptography?

- **Secret key cryptography**
  - ◆ Requires secure channel for key distribution
  - ◆ *In principle* every classical channel can be monitored passively
  - ◆ Security is mostly based on complicated non-proven algorithms
- **Public key cryptography**
  - ◆ Security is based on non-proven mathematical assumptions (e.g. difficulty of factoring large numbers)
  - ◆ We DO know how to factorize in polynomial time! Shor's algorithm for quantum computers. Just wait until one is built.
  - ◆ Breakthrough renders messages insecure *retroactively*



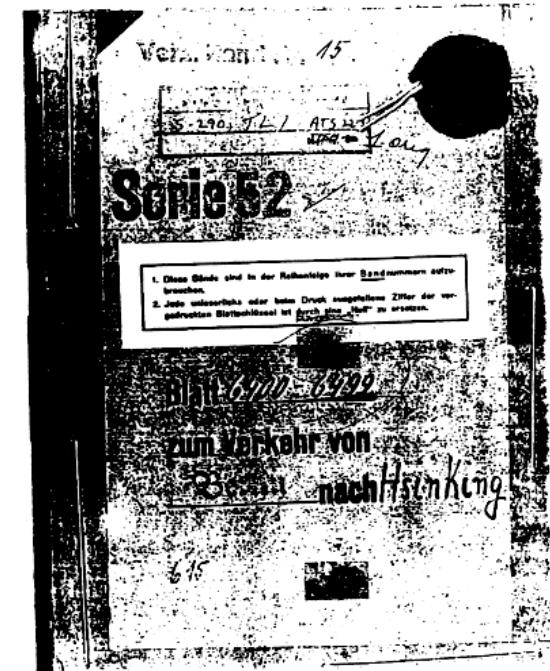
# The holy grail: One-time pad

- The only cipher mathematically proven
- Requires massive amounts of key material



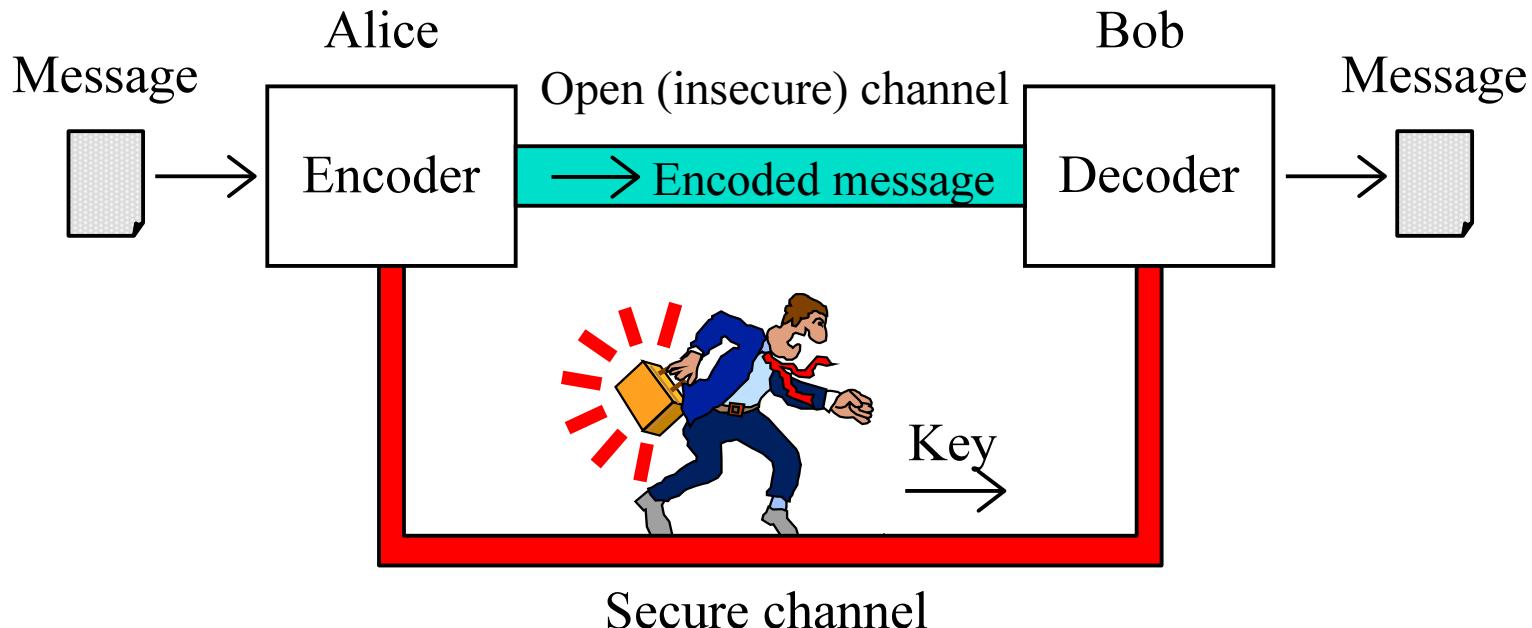
6451

76168	93947	44636	47649	83481	03137
29660	52537	72742	00121	80078	27567
66724	35079	44598	76371	29837	70579
43632	72103	80867	17661	27430	71118
72957	55168	45432	49696	26698	31812
25320	76236	91254	50685	76351	40993
00799	41393	21453	96296	89065	4246
49024	58205	11294	99980	36393	24309



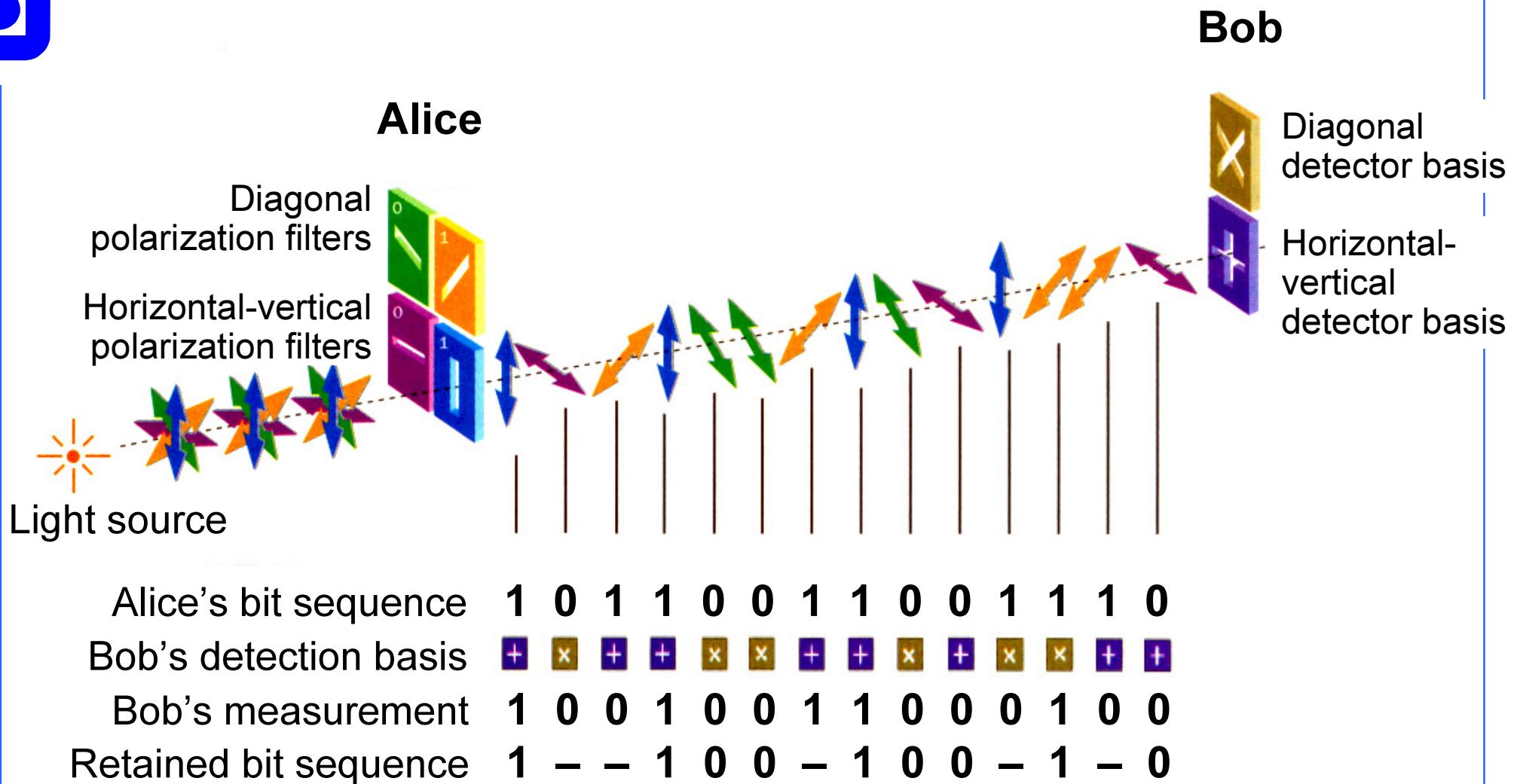


# Key distribution



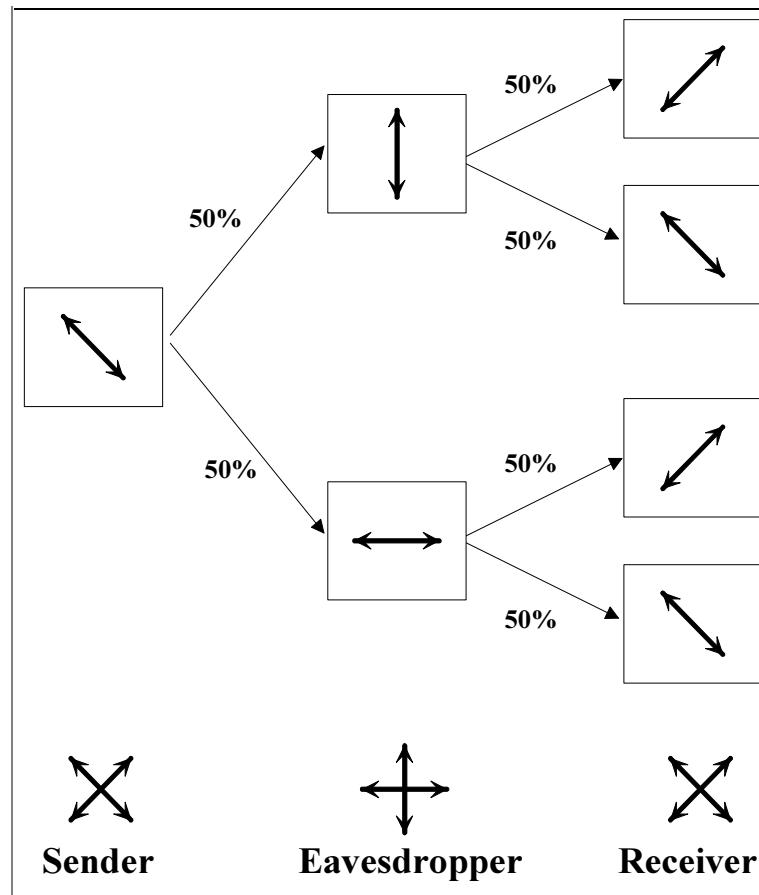
- **Secret key cryptography requires secure channel for key distribution.**
- **Quantum cryptography distributes the key by transmitting quantum states in *open channel*.**

# Quantum key distribution





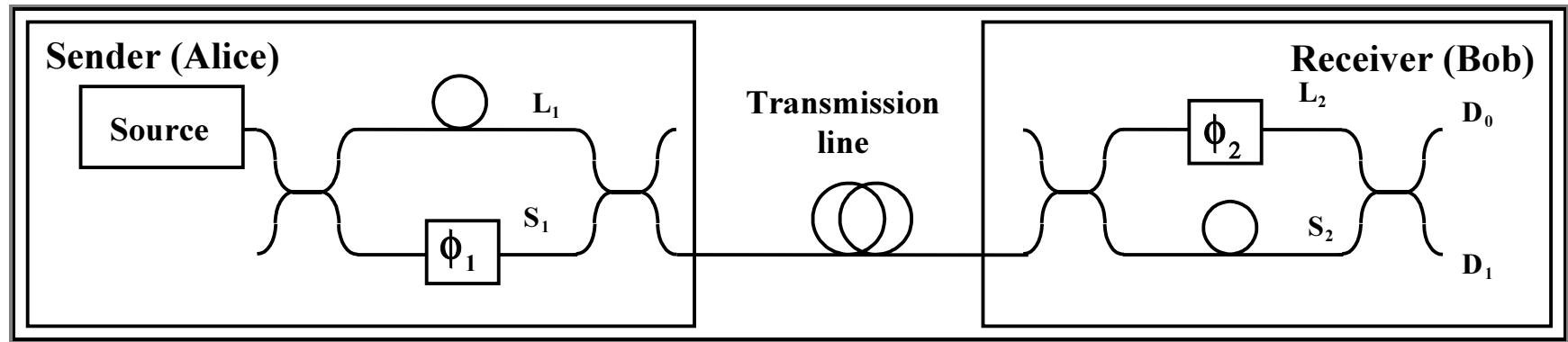
# Eavesdropping with wrong reference system



Sender	Tyvlytter		Mottaker
	Referanse	Resultat av måling	
"0"	Rett	"0"	Rett
	Galt	"0"	Rett Galt
"1"	Rett	"1"	Rett
	Galt	"0"	Rett Galt
"0"	Rett	"1"	Rett
	Galt	"1"	Rett Galt
	Rett	"0"	Rett Galt
"1"	Rett	"1"	Rett
	Galt	"1"	Rett Galt
	Rett	"0"	Rett Galt



# Interferometric QKD channel



$$\phi_1 = 0^\circ \text{ or } 90^\circ - "1"$$

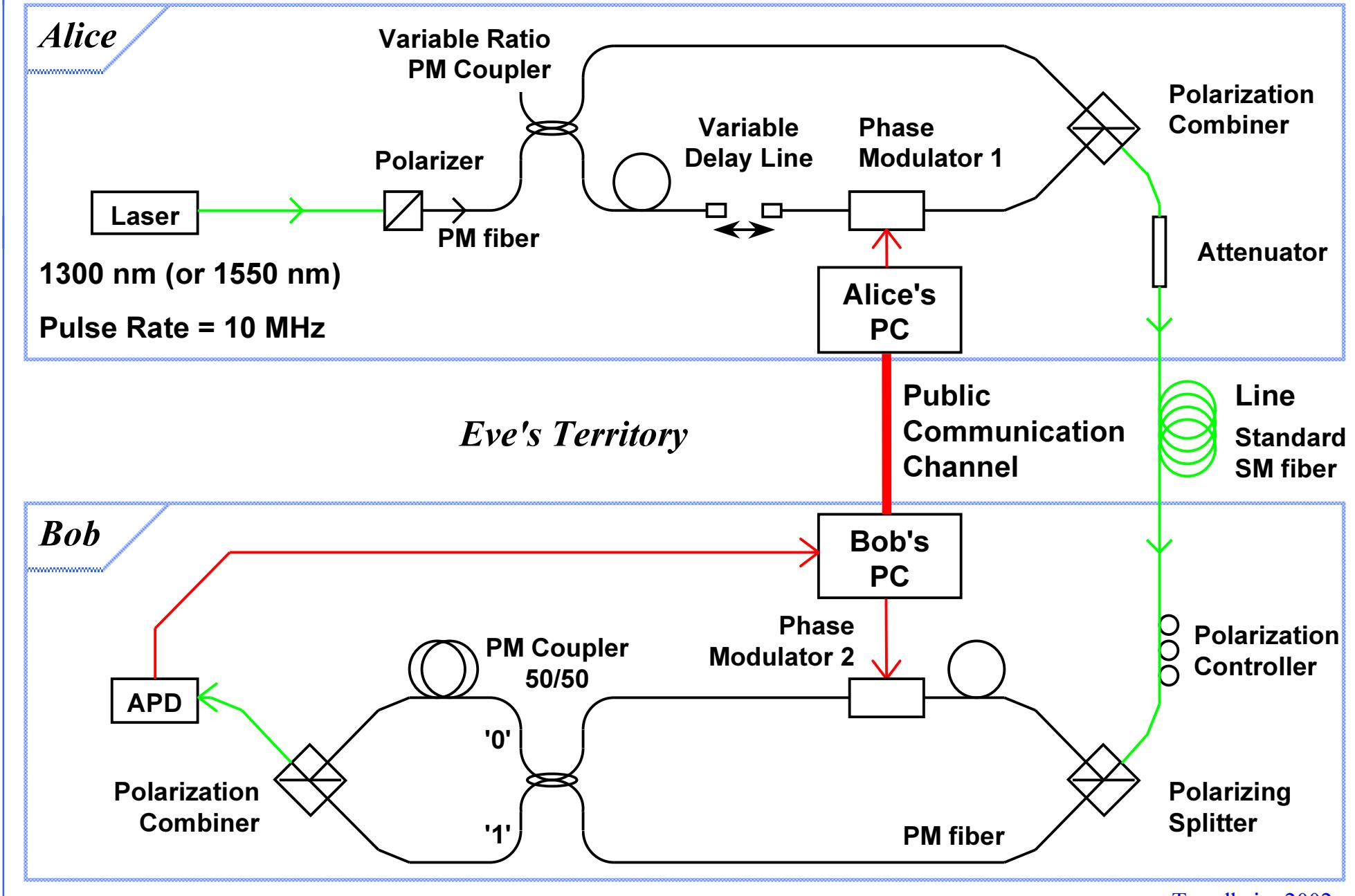
$$\phi_1 = 180^\circ \text{ or } 270^\circ - "0"$$

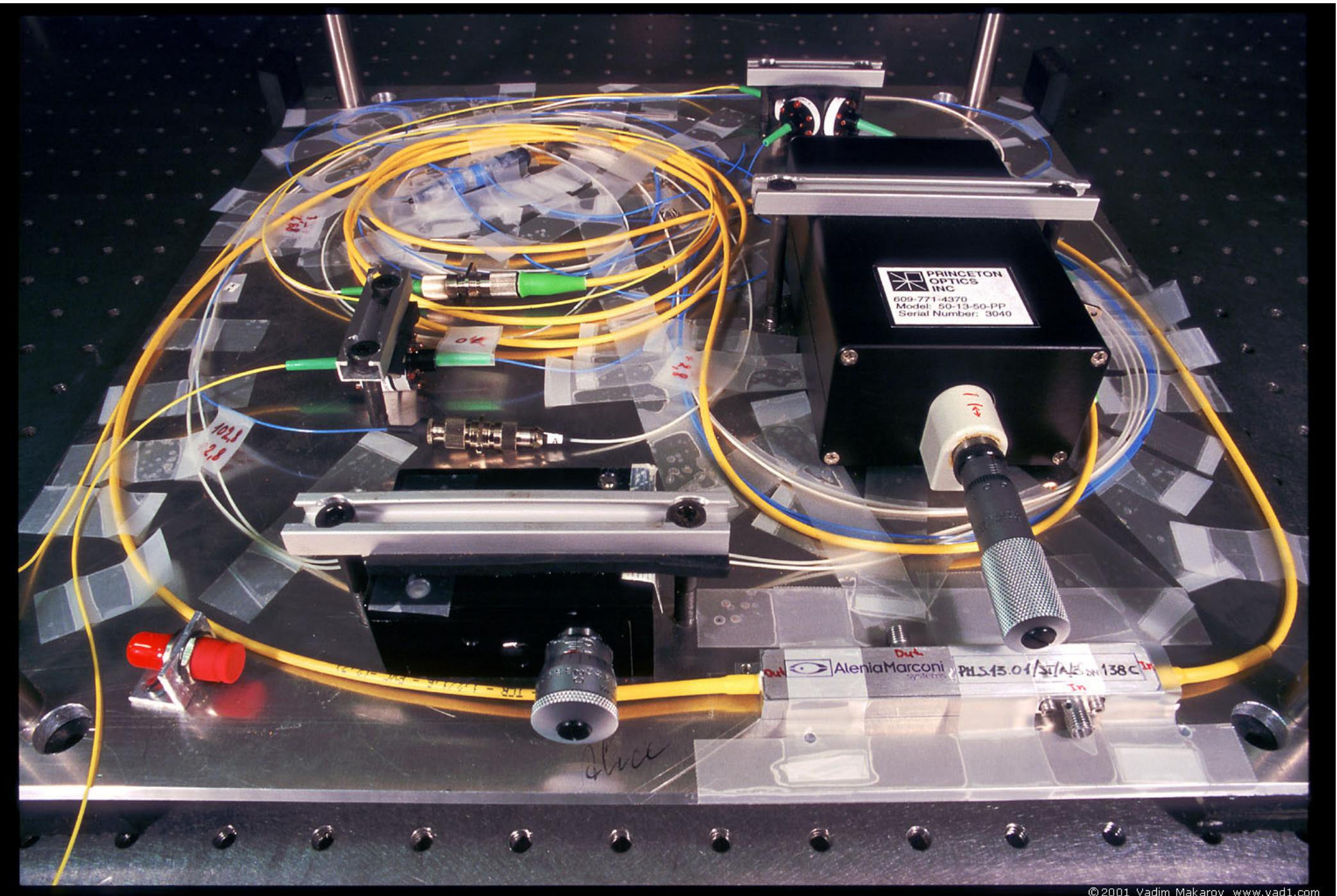
Reference  
systems:

$$\phi_2 = 0^\circ$$

$$\phi_2 = 90^\circ$$

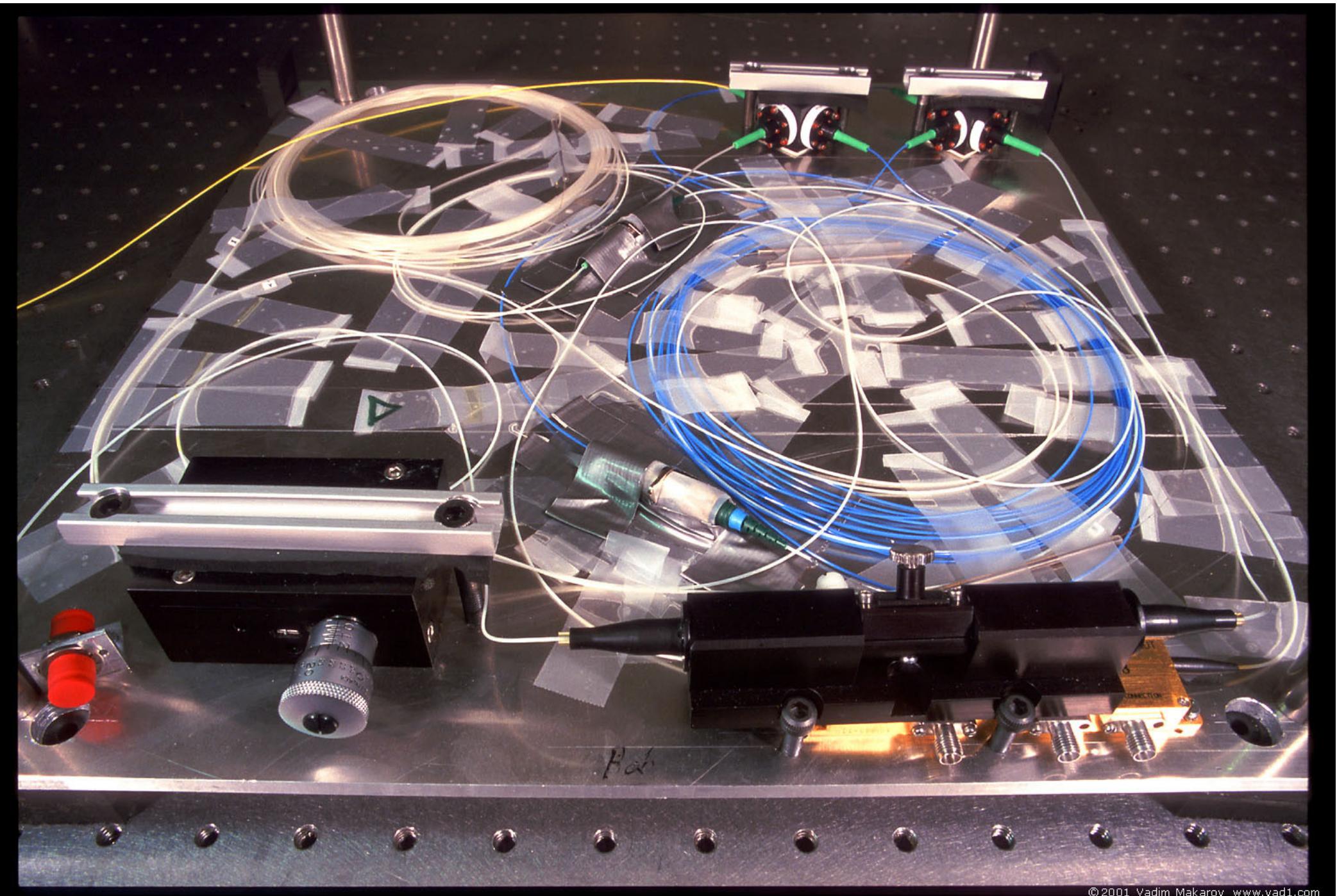
# Implementation: interferometer structure





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Photo 1. Alice (uncovered, no thermoisolation installed)

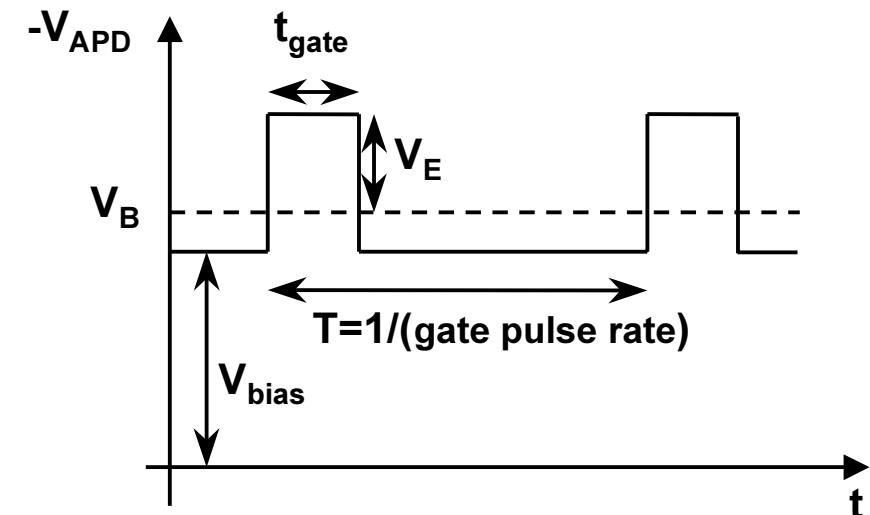
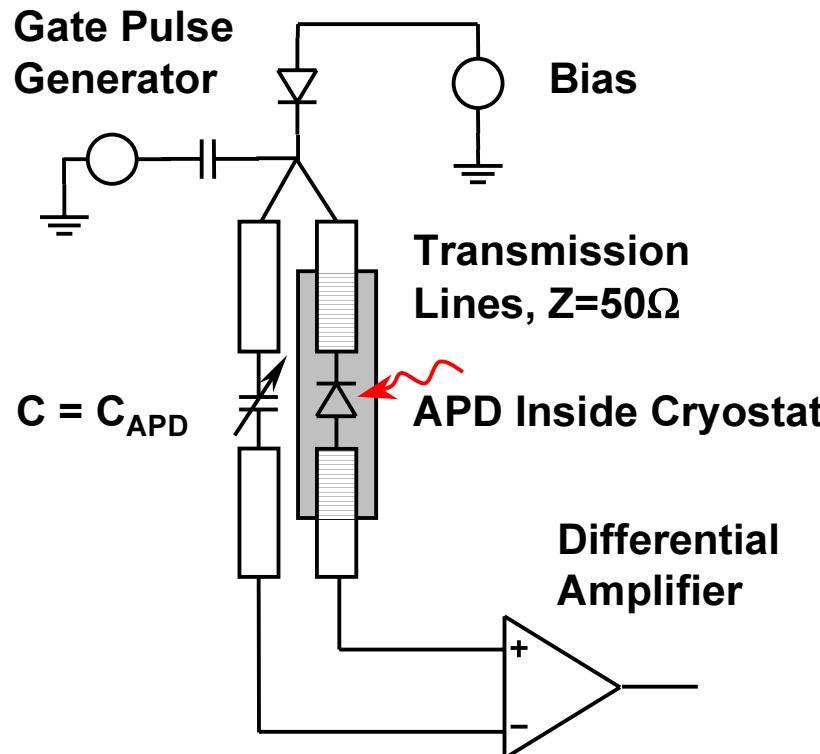


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Photo 2. Bob (uncovered, no thermoisolation installed)



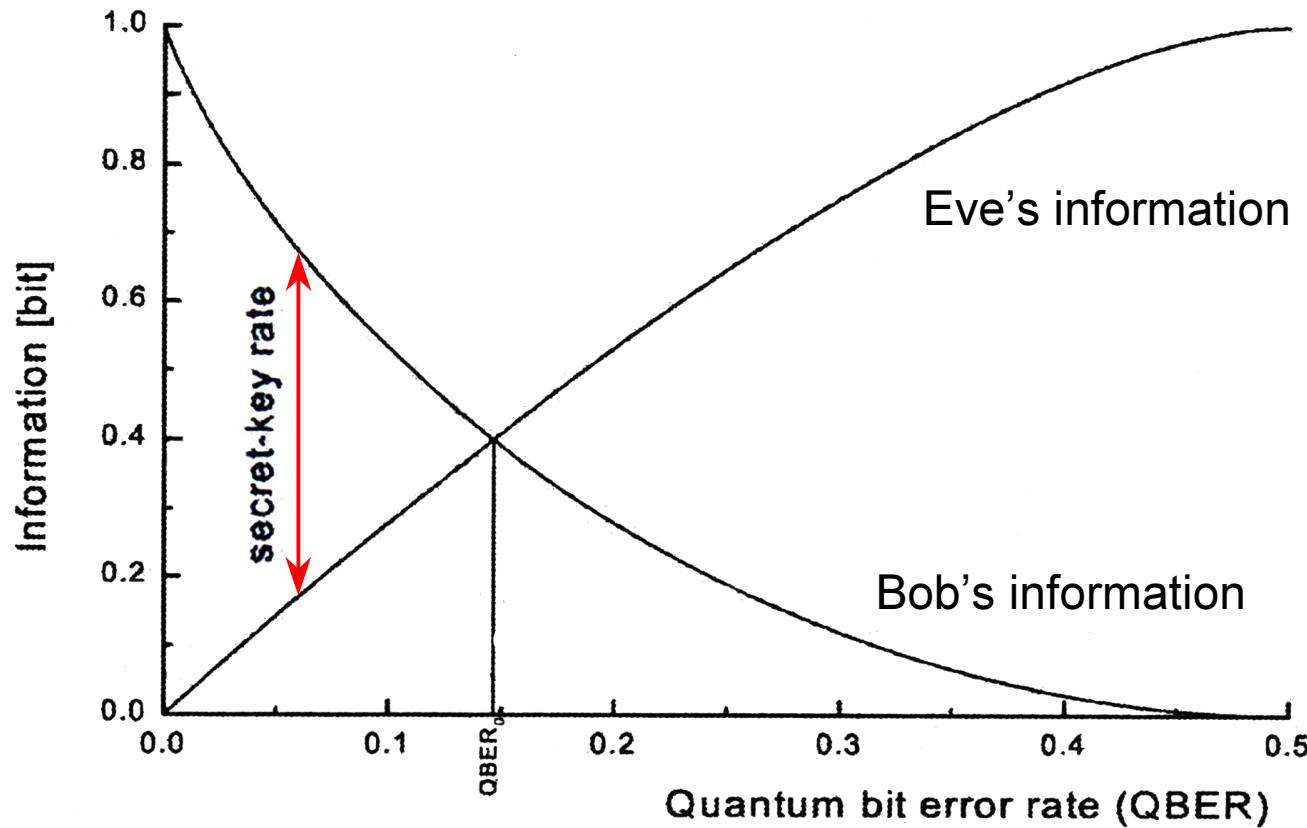
# Single-photon detector: APD in Geiger mode



$t_{gate}$  down to 1ns  
gate pulse rate = 20 MHz



# Recovery from errors



QBER limit:

- Individual attacks: 15%
- All theoretically possible attacks: 11%

# Distance limitation

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Maximum link distance, km

70

30

20

5

0

5E-5

Few %

Detector noise level  
(dark count probability)

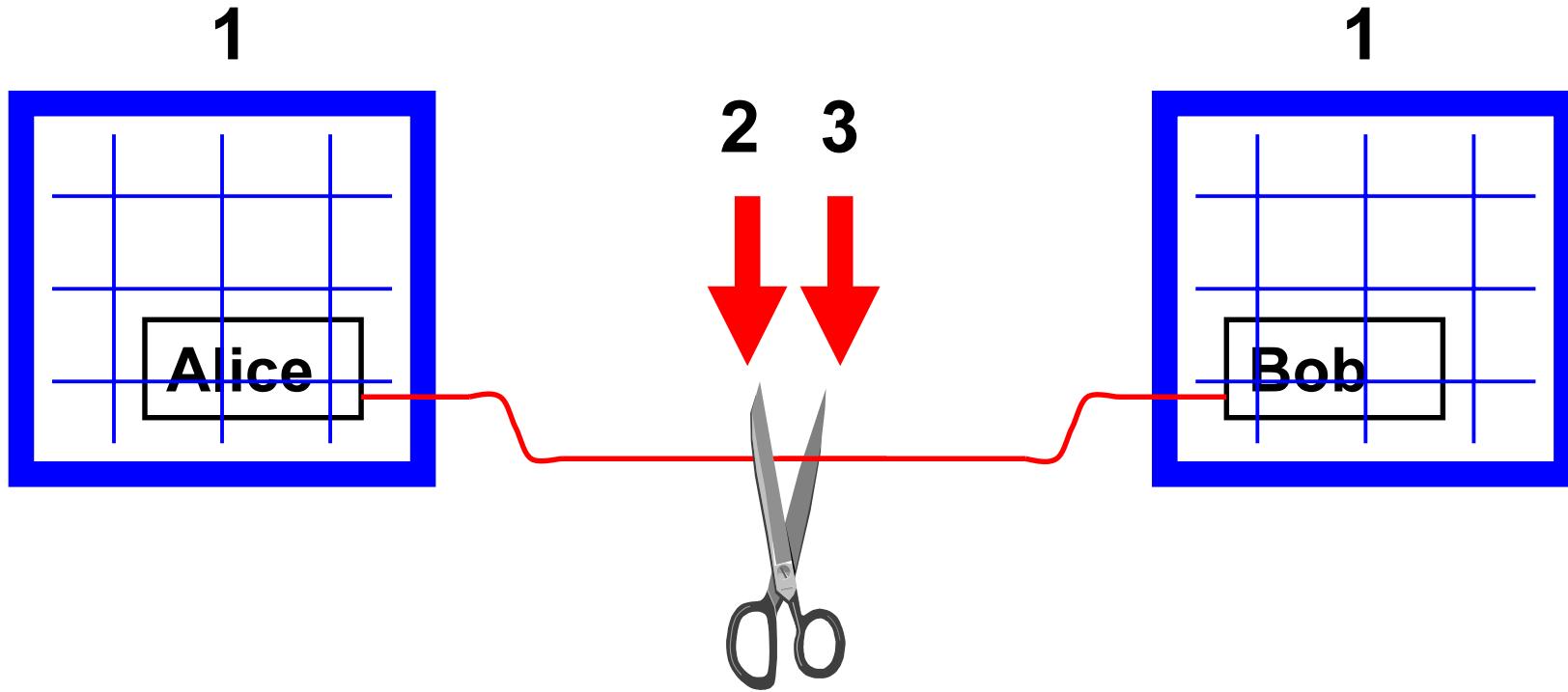
1550 nm

1300 nm

850 nm

$\lambda$ , nm	Fiber attenuation, dB/km	Detectors
850	2	Si, room temperature
1300	0.35	Ge, -196°C
1550	0.2	InGaAs, ~ -60°C

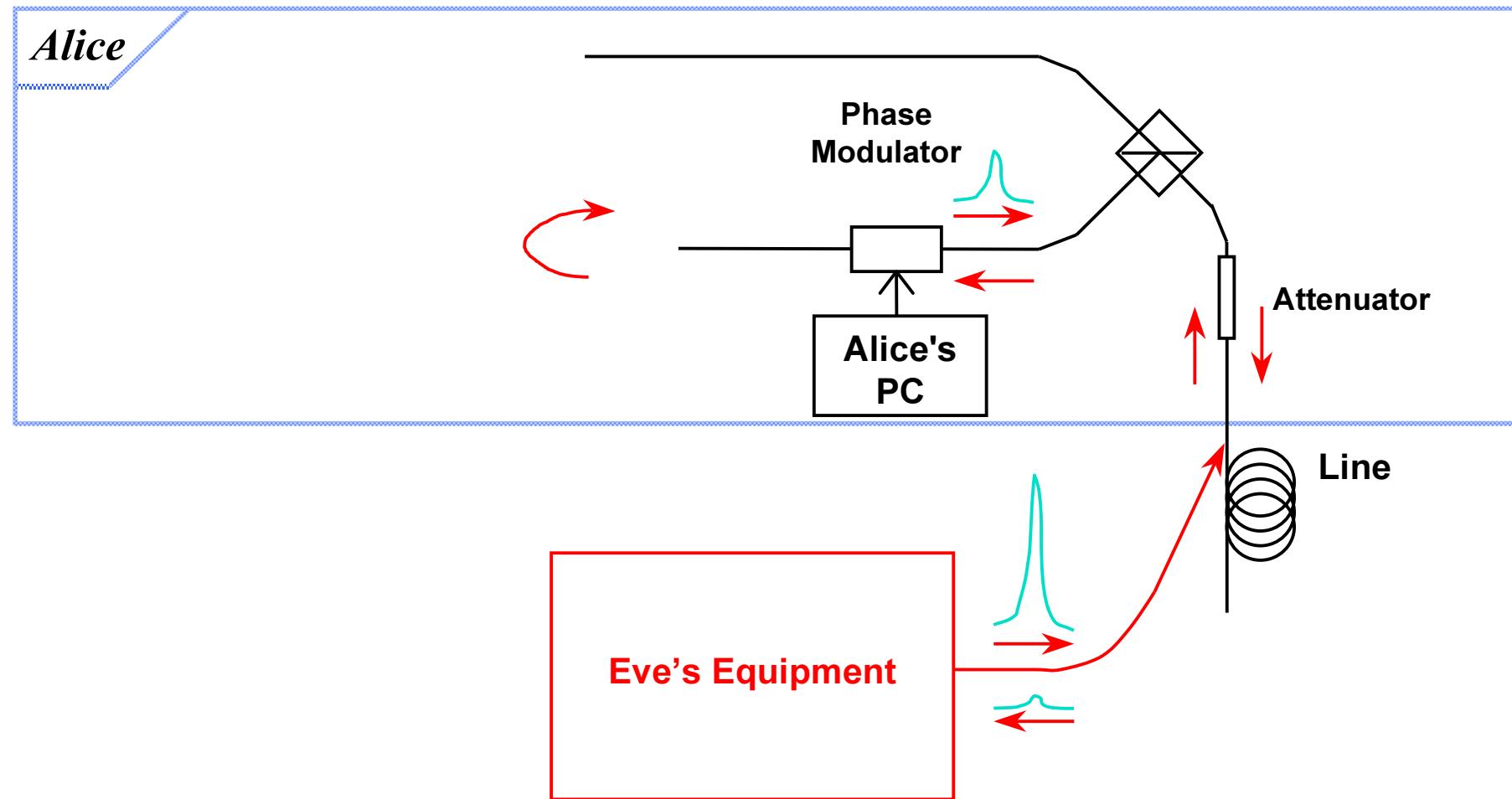
# Components of security



1. Conventional security
2. Security against quantum attacks
3. Security against Trojan horse attacks
  - ones that don't deal with quantum states, but use loopholes in optical scheme

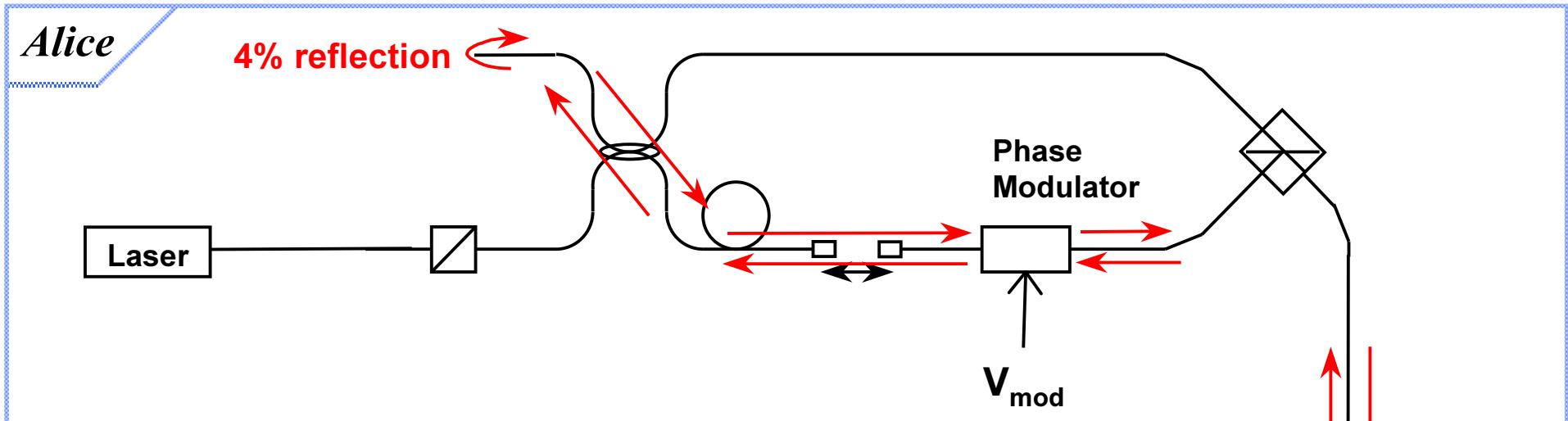
# Practical security: large pulse attack

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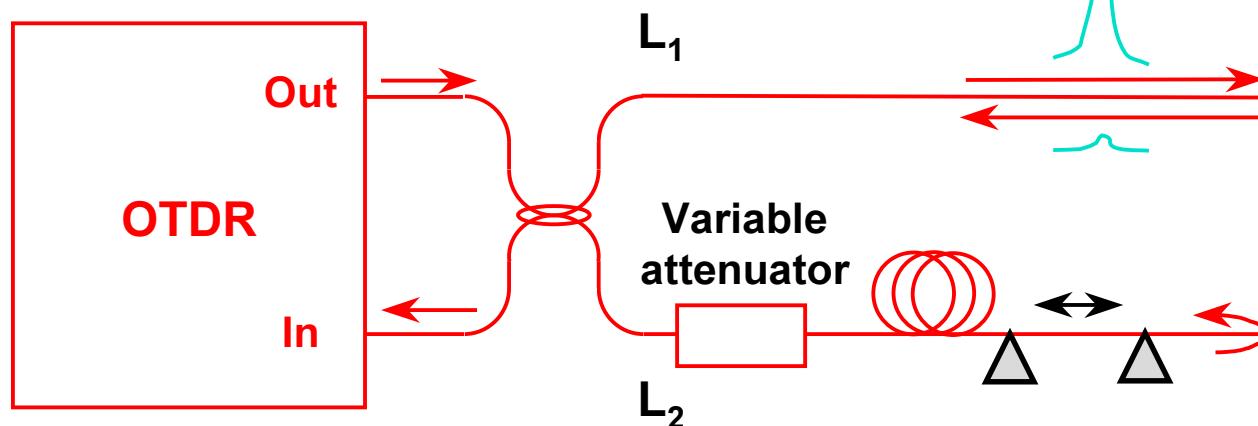


- interrogating Alice's phase modulator with powerful external pulses  
(can give Eve bit values directly)

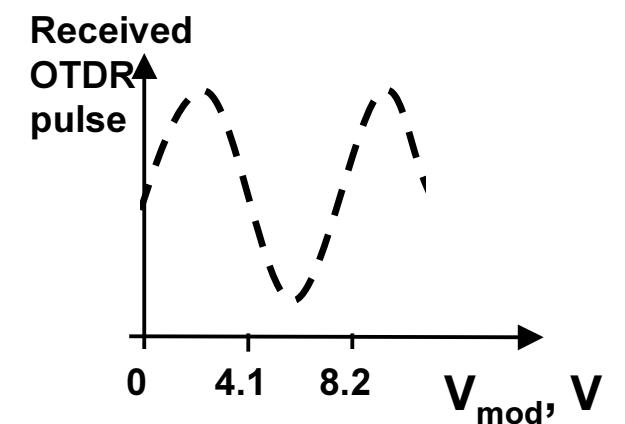
# Eavesdropping experiment



*Eve*



Fine length  
adjustment  
to get  $L_1 = L_2$



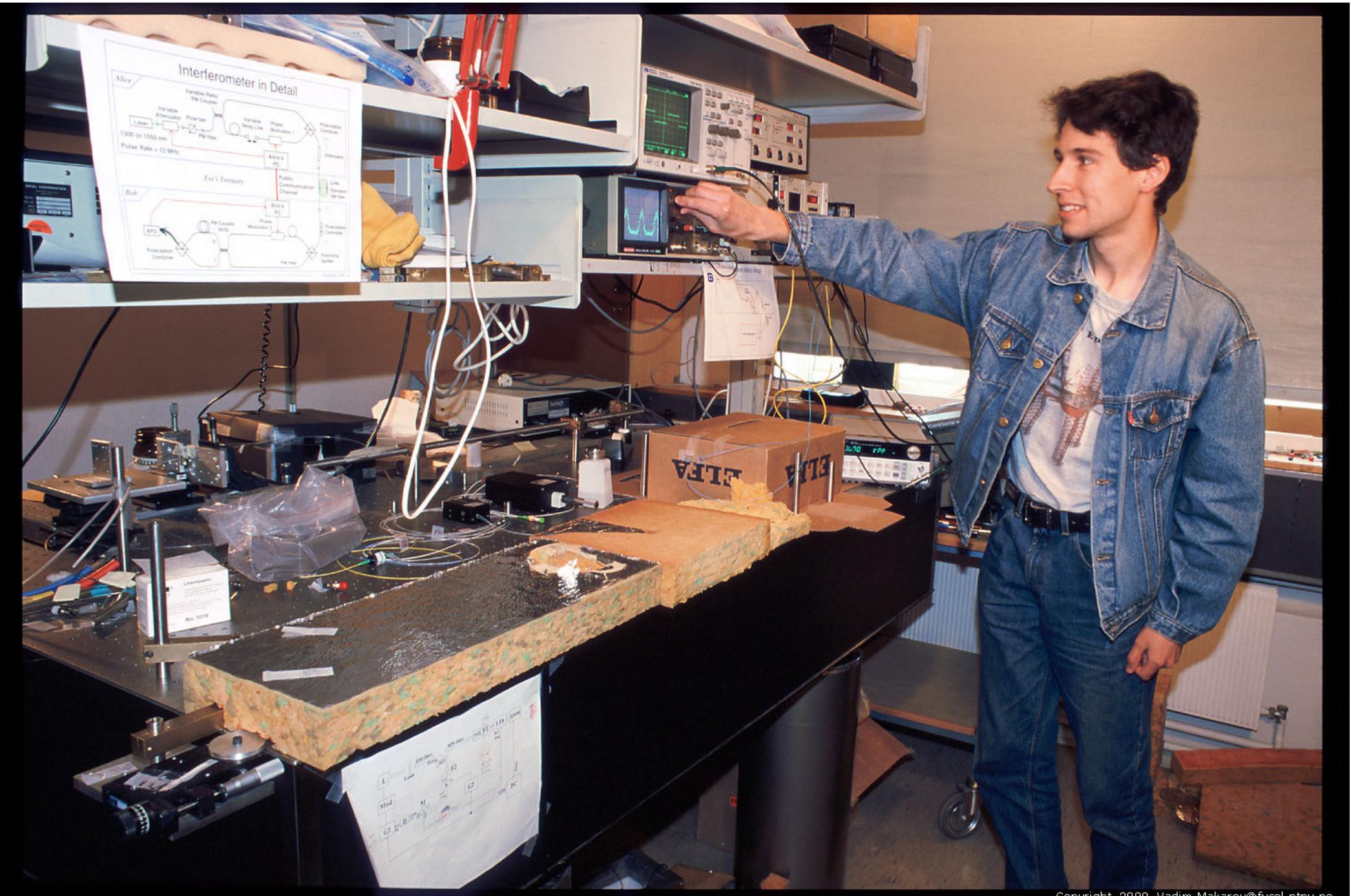
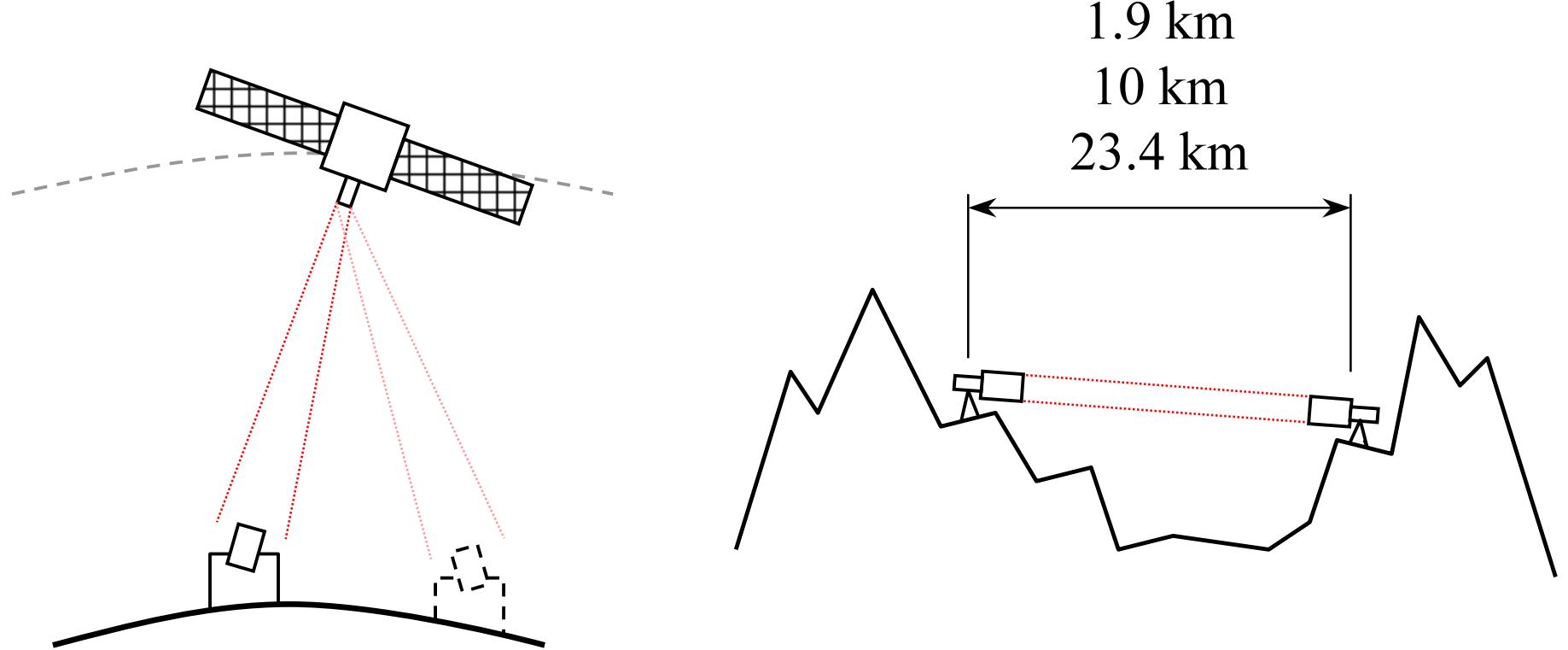


Photo 3. Artem Vakhitov tunes up Eve's setup

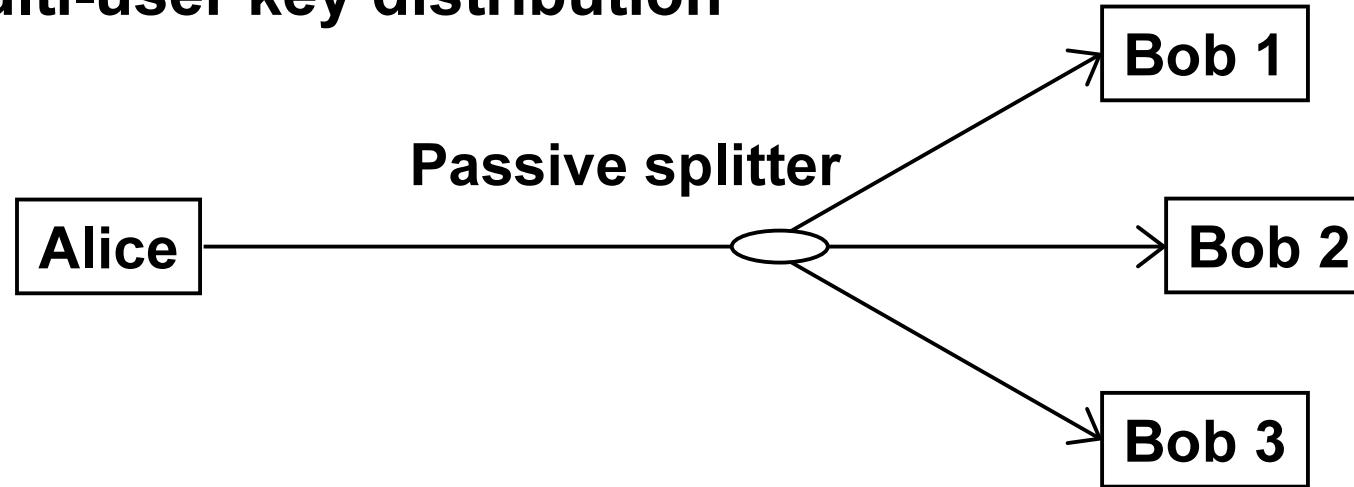


# Re-keying satellites/ Global key distribution network

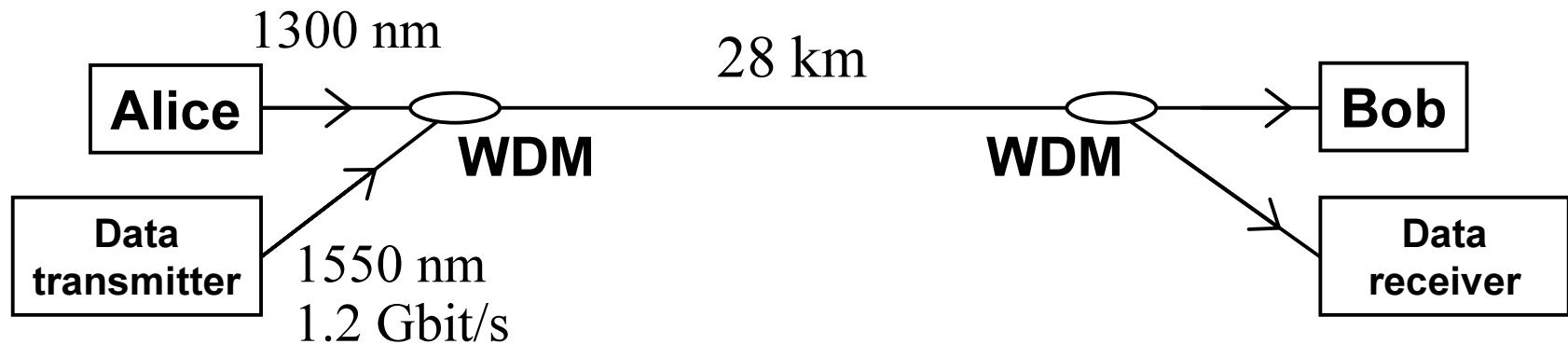


# Quantum key distribution in network

- Multi-user key distribution

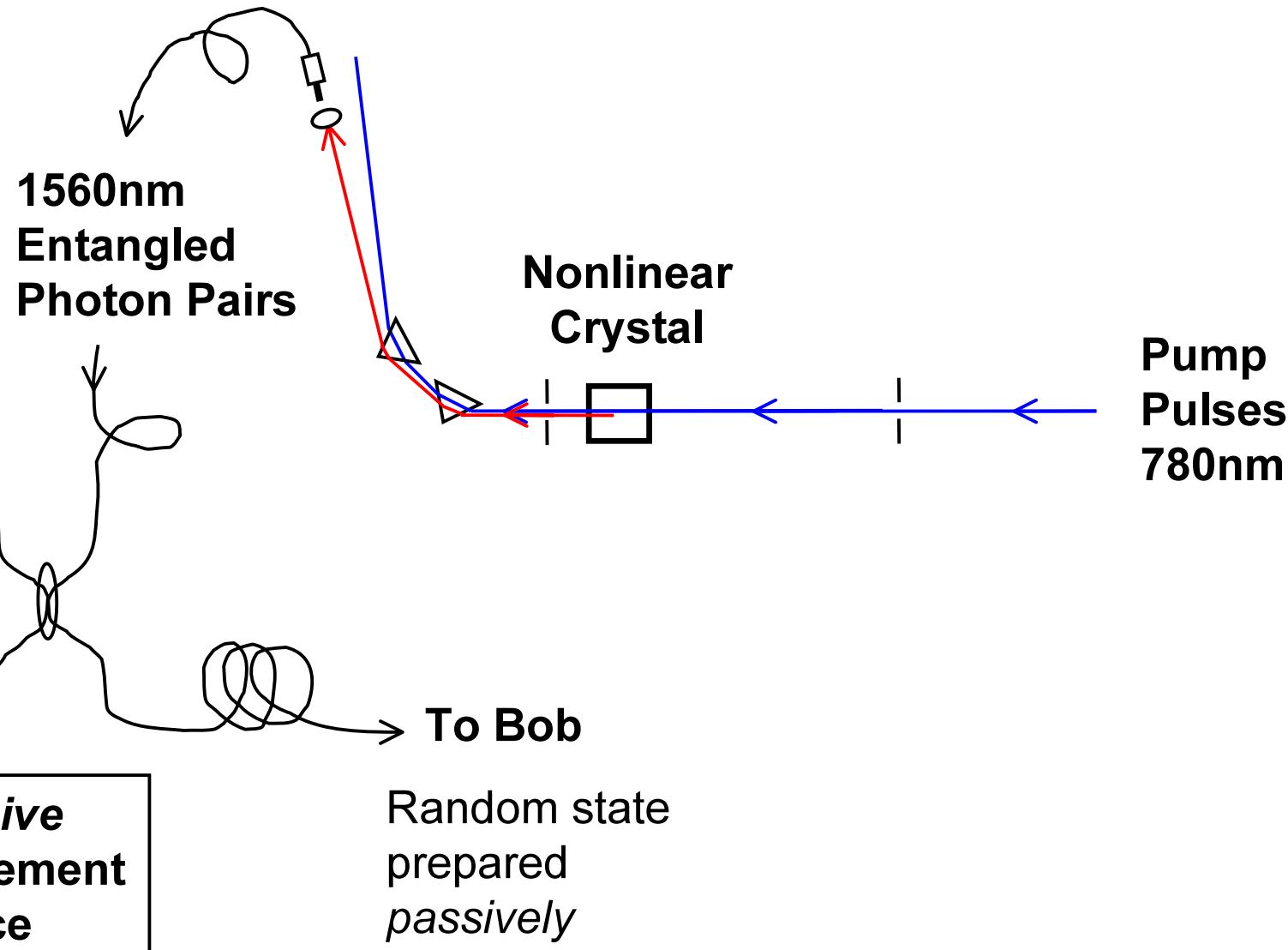


- Multiplexing with telecom traffic

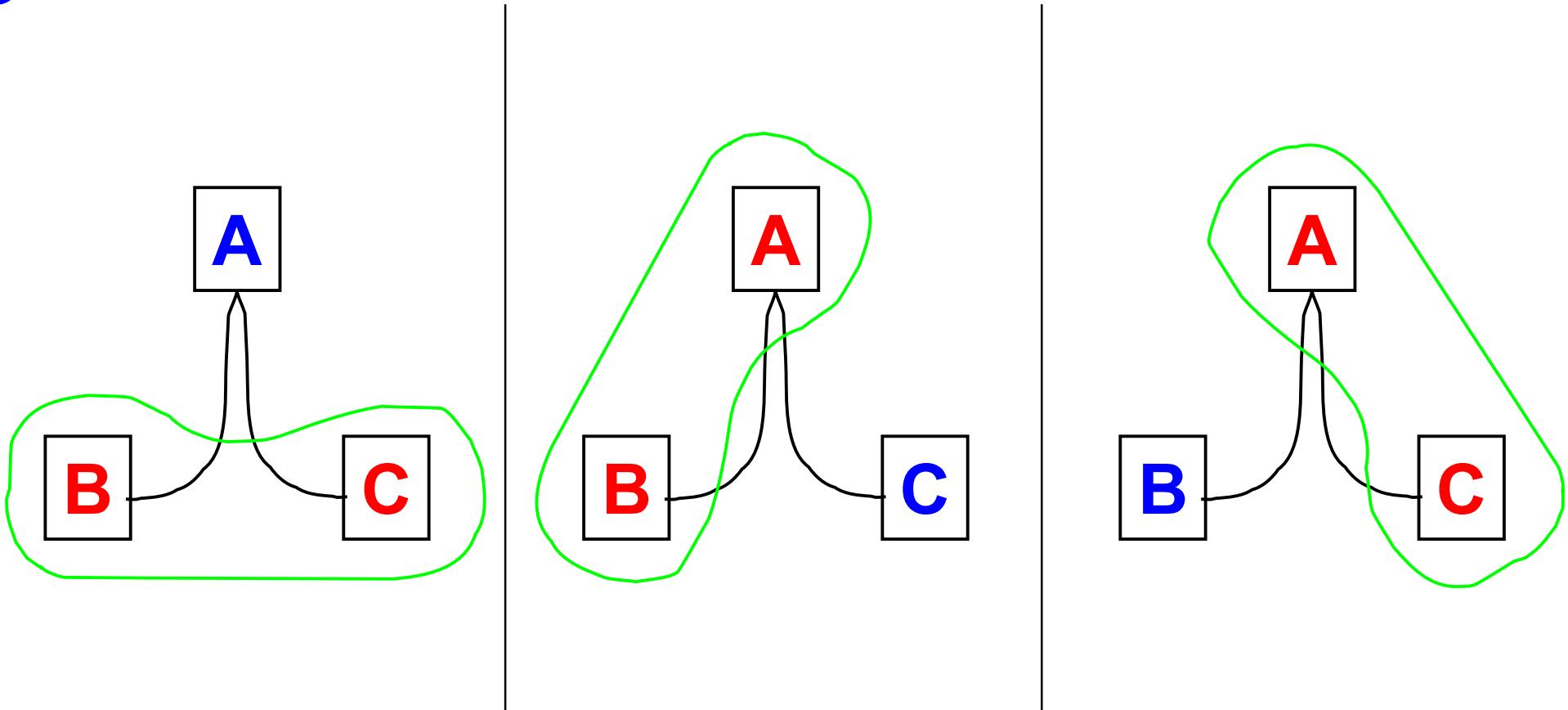


# Entangled photon pairs

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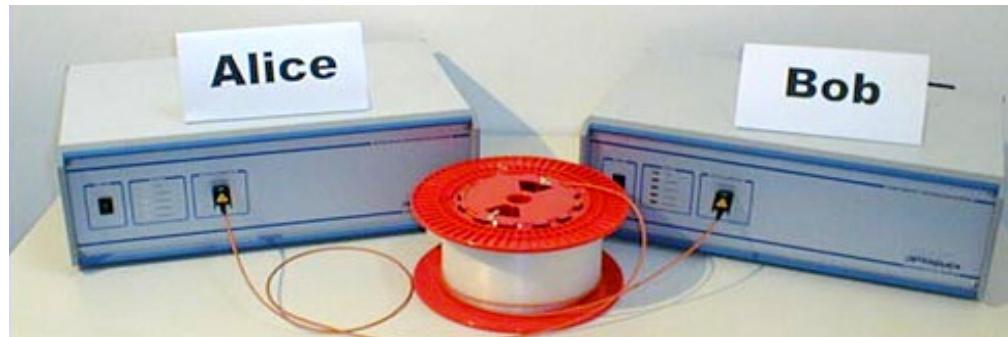
# Advanced multi-party protocols: Secret sharing and splitting



# Commercial status



- **id Quantique (Geneva)**  
first commercially available quantum key distribution system:



- **MagiQ Technologies (Boston)**
- **EQUIS project (Heriot-Watt University and Corning; UK)**  
compact integration into standard PCs
- + several research groups, telecom/ electronics companies