

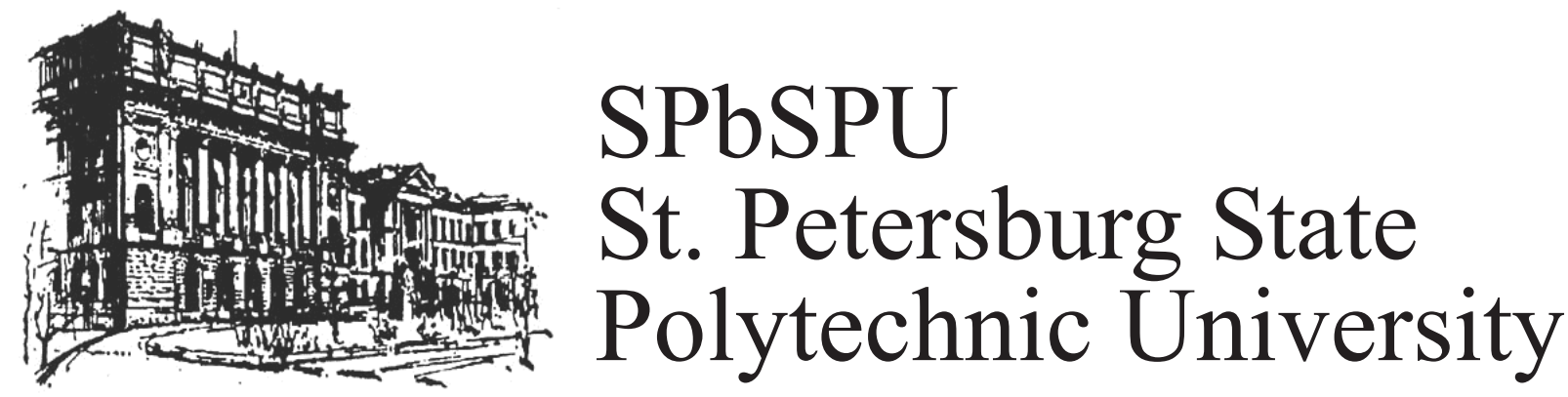


Faked states attack exploiting detector efficiency mismatch on BB84, phase-time, DPSK, and Ekert protocols

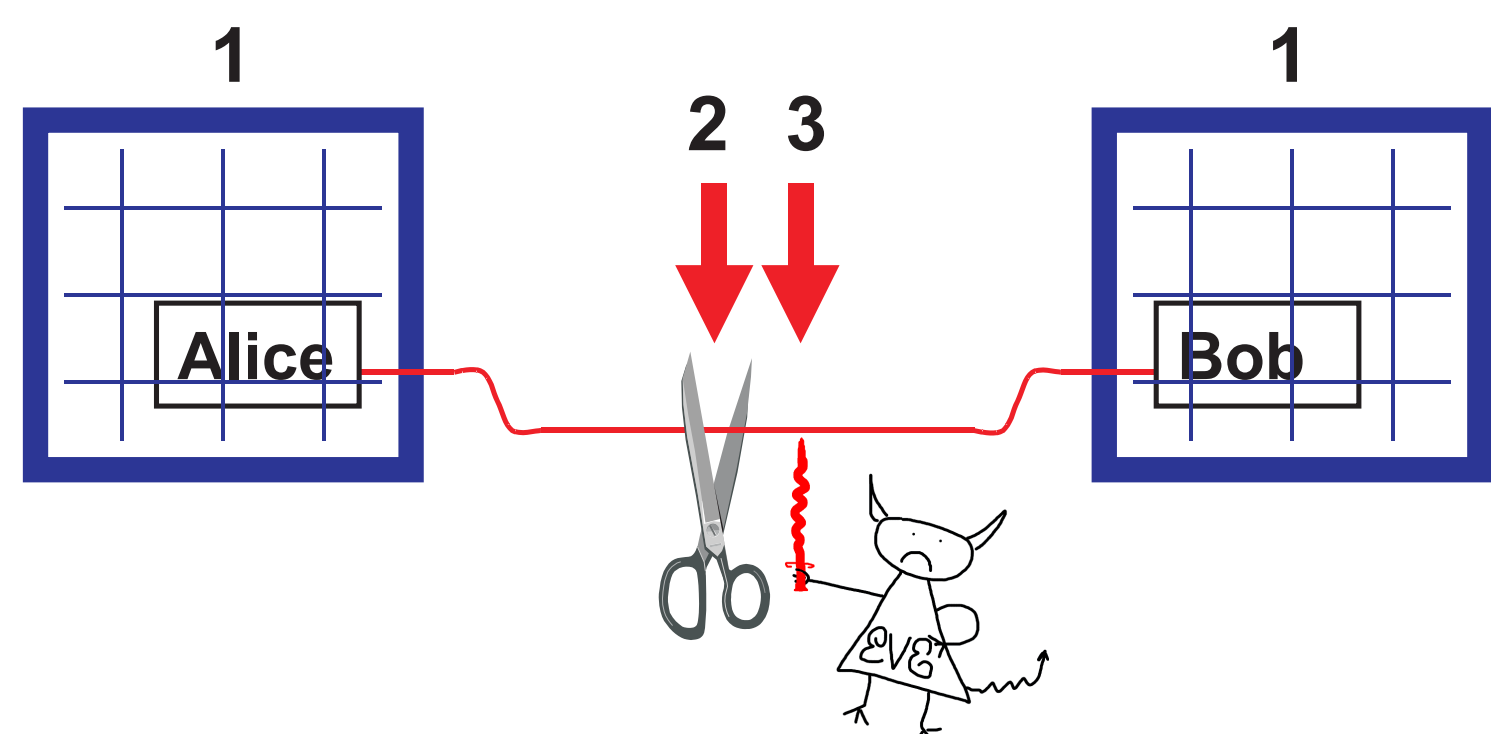
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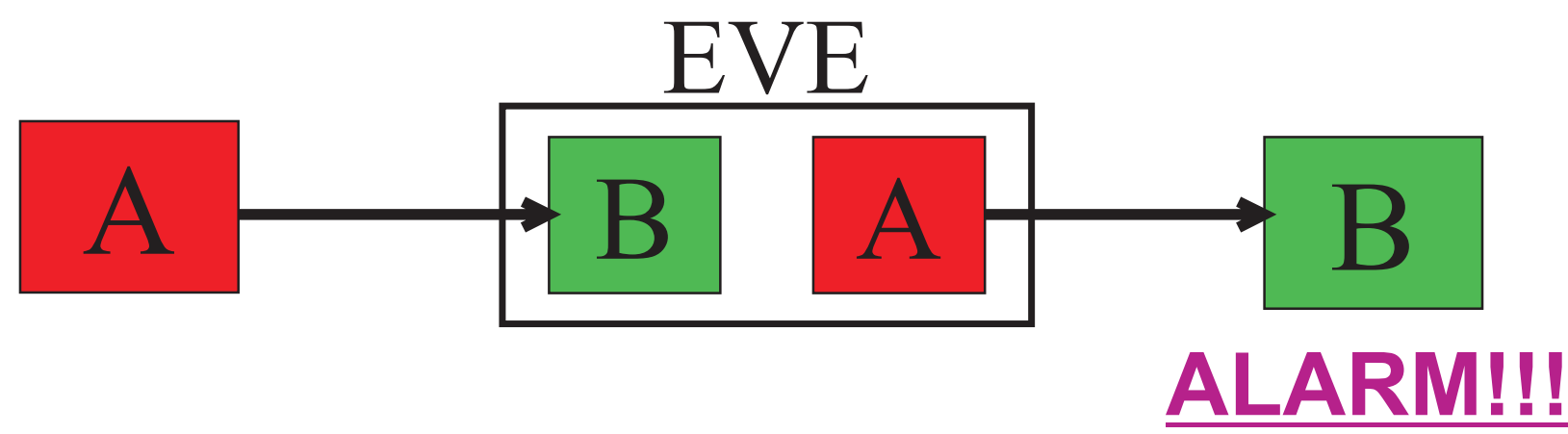
Quantum key distribution: components of security



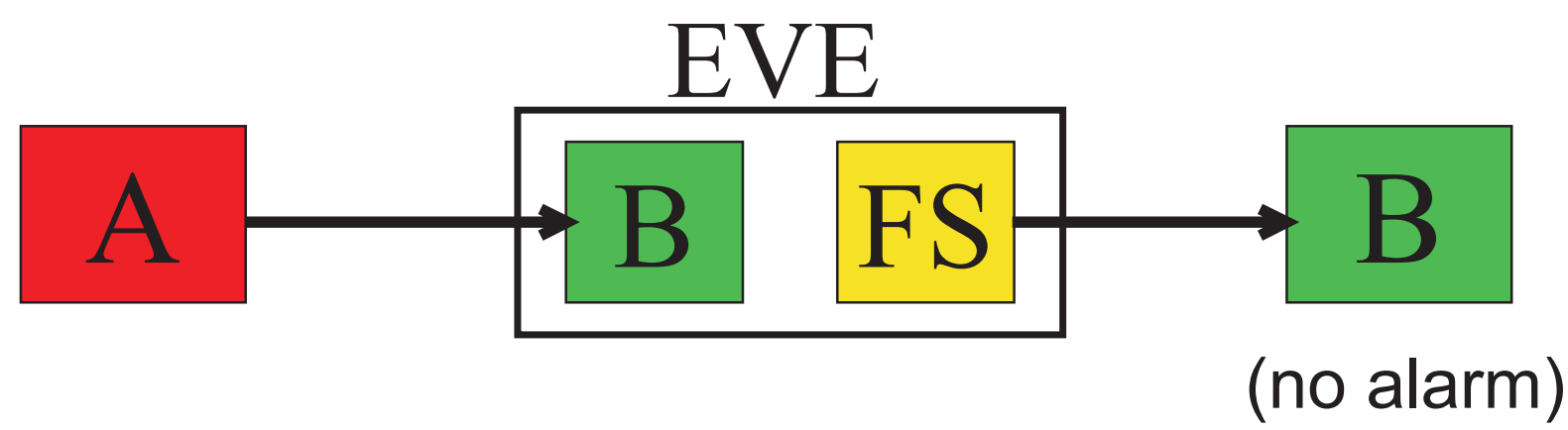
1. **Conventional security; trusted equipment manufacturer**
2. **Security against quantum attacks**
3. **Loopholes in optical scheme**
 - attacks that don't deal with quantum states, but use loopholes and imperfections in implementation

Faked states attack

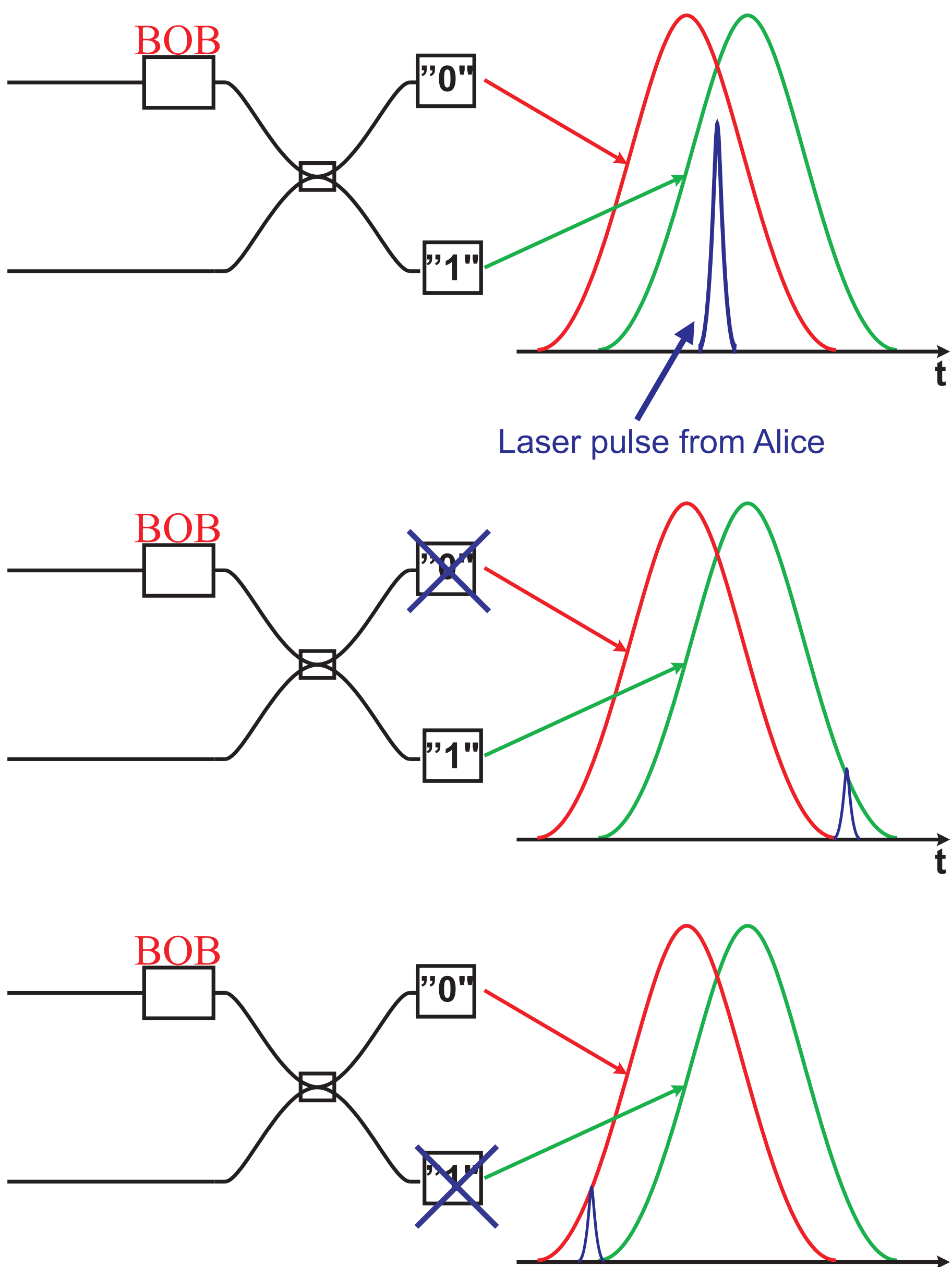
Conventional intercept/resend:



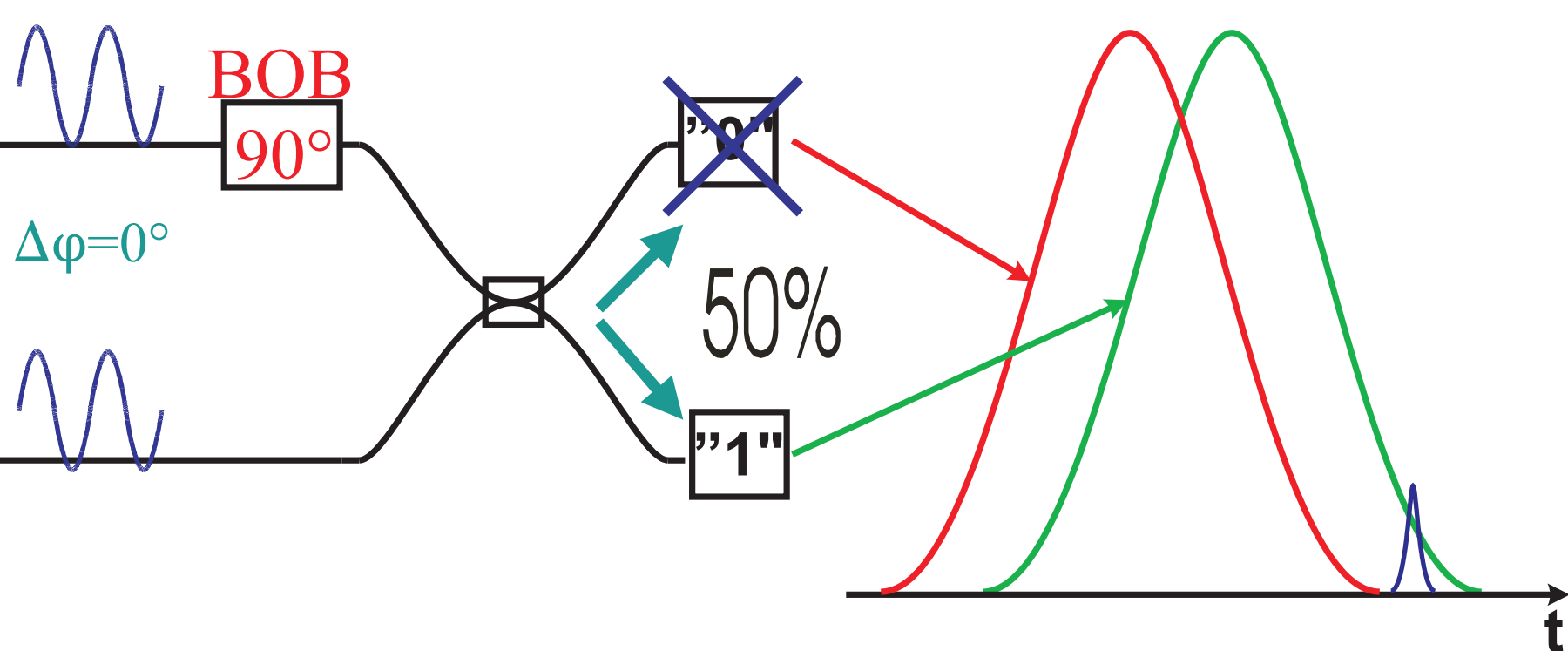
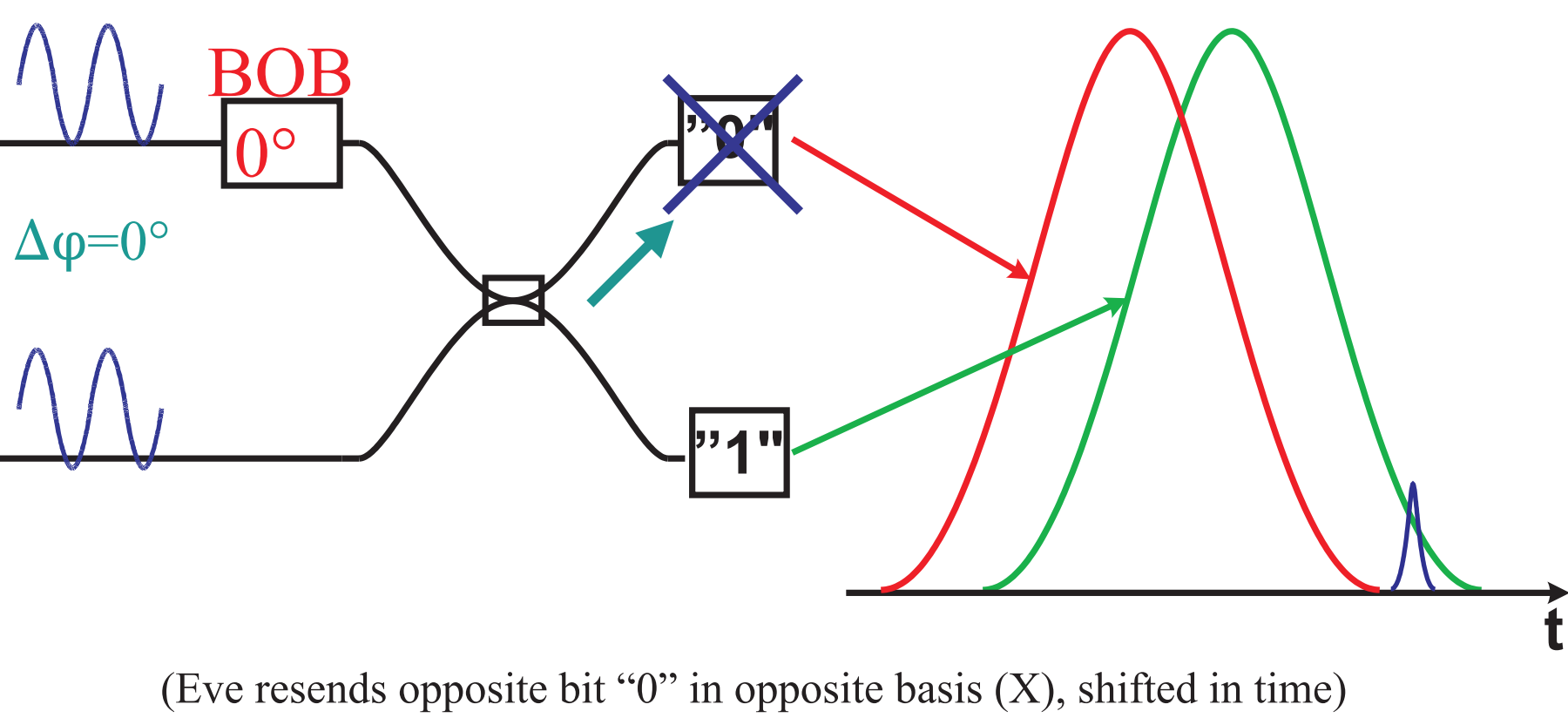
Faked states attack:



Exploiting common imperfection: detector gate misalignment

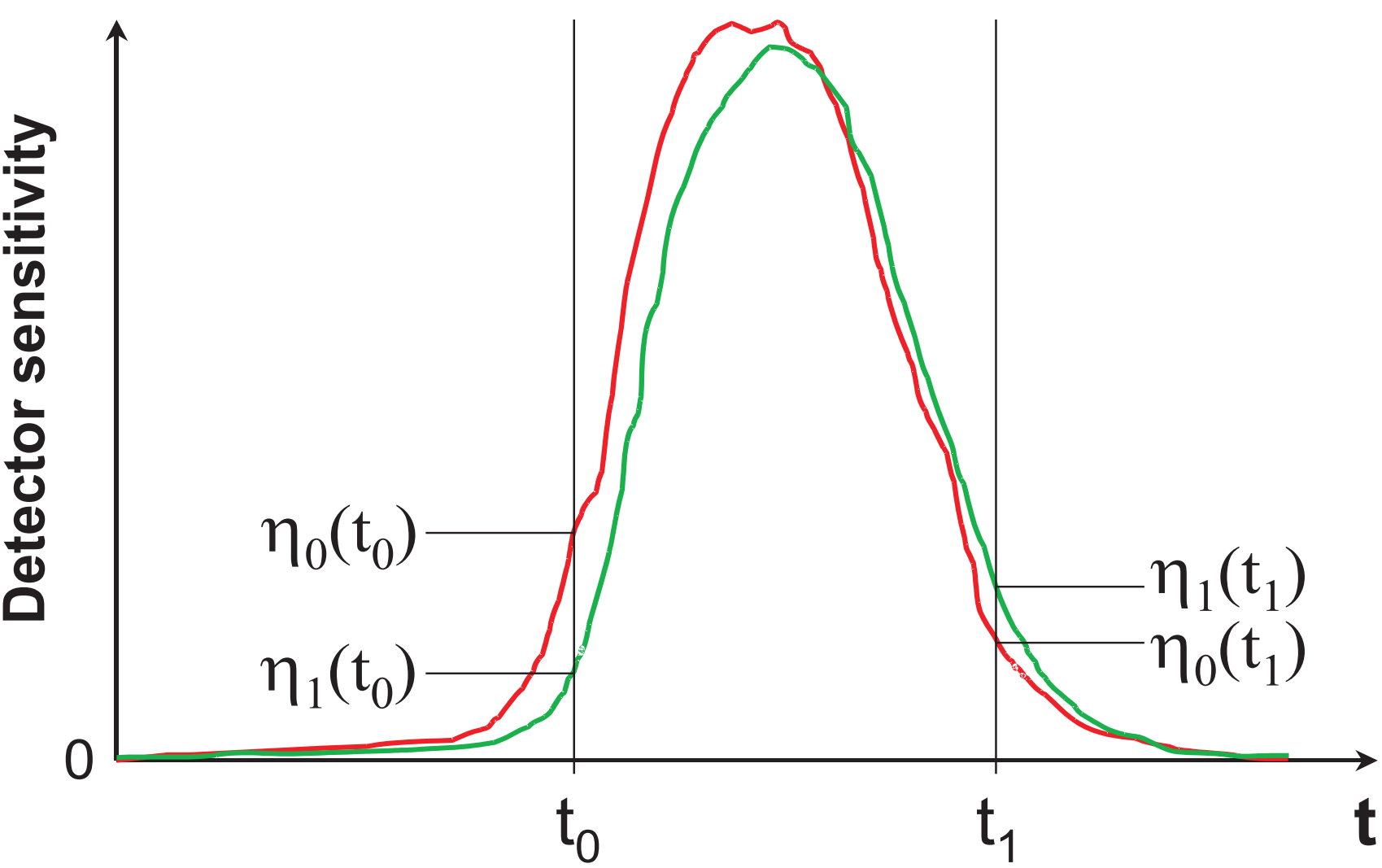


Example: Eve measured with basis Z (90°), obtained bit "1"



- ✓ Eve's attack is not detected
- ✓ Eve obtains 100% information of the key

Partial sensitivity mismatch



A. Practical intercept-resend attack

Alice → Eve	Eve → Bob	Bob	Probability	Sifting
Z0	Z0	X1t0	Z 0, 1, 1/2 η0(t0)	keep
Z0	Z0	X1t0	X 0, 1, 1/2 η1(t0)	keep
Z0	Z0	X1t0	–, 1 – 1/2 η0(t0) – 1/2 η1(t0)	lost
Z0	Z0	X1t0	X 0, 1, 1/2 η0(t0)	discard
Z0	Z0	X1t0	–, 1 – η1(t0)	lost
Z0	Z0	X1t0	Z 0, 1, 1/2 η0(t0)	keep
Z0	Z0	X1t0	–, 1 – 1/2 η0(t0) – 1/2 η1(t0)	lost
Z0	Z0	X1t0	X 0, 1, 1/2 η0(t0)	discard
Z0	Z0	X1t0	–, 1 – η1(t0)	lost
Z0	X0	Z1t0	Z 0, 1, 1/2 η0(t0)	keep
Z0	X0	Z1t0	X 0, 1, 1/2 η1(t0)	keep
Z0	X0	Z1t0	–, 1 – 1/2 η0(t0) – 1/2 η1(t0)	lost
Z0	X0	Z1t0	X 0, 1, 1/2 η0(t0)	discard
Z0	X0	Z1t0	–, 1 – η1(t0)	lost
Z0	X1	Z0t1	Z 0, 1, 1/2 η0(t1)	keep
Z0	X1	Z0t1	X 0, 1, 1/2 η1(t1)	keep
Z0	X1	Z0t1	–, 1 – 1/2 η0(t1) – 1/2 η1(t1)	lost

$$\text{QBER} = \frac{P(\text{error})}{P(\text{arrive})} = \frac{2\eta_0(t_1) + 2\eta_1(t_0)}{\eta_0(t_0) + 3\eta_0(t_1) + 3\eta_1(t_0) + \eta_1(t_1)}$$

In the symmetric case $\frac{\eta_1(t_0)}{\eta_0(t_0)} = \frac{\eta_0(t_1)}{\eta_1(t_1)} = \eta$

For $\eta \leq 0.066$ (~ 1:15), QBER $\leq 11\%$.

Eve can compromise security if mismatch is larger than 1:15

B. General security bound

Secure key generation rate:

$$R = 1 - 2h(\delta),$$

where δ is the actual bit error rate.

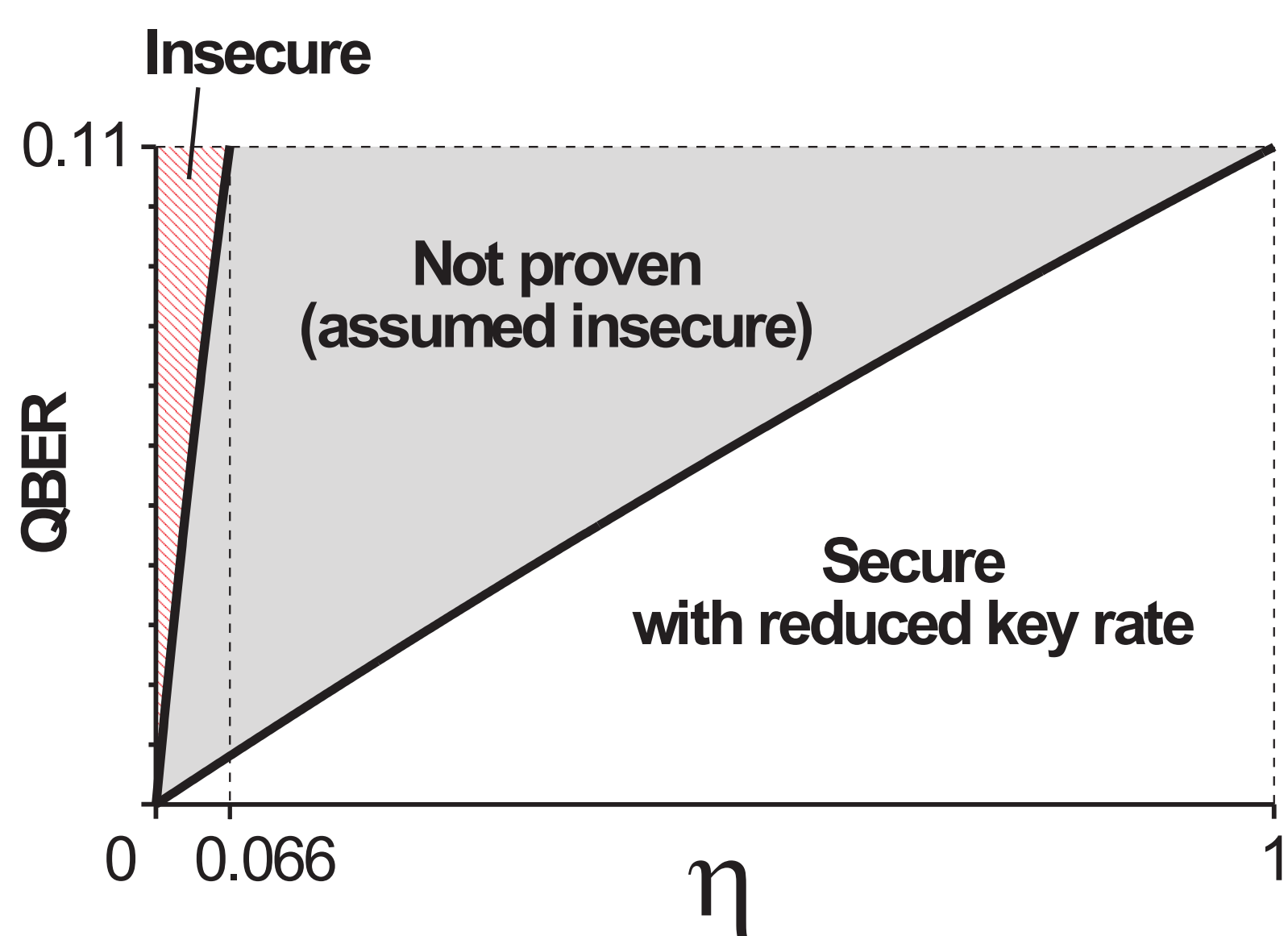
For $\eta_0(t) \neq \eta_1(t)$,

$$\text{QBER} = \frac{\eta\delta}{1 + \eta\delta - \delta} \approx \eta\delta,$$

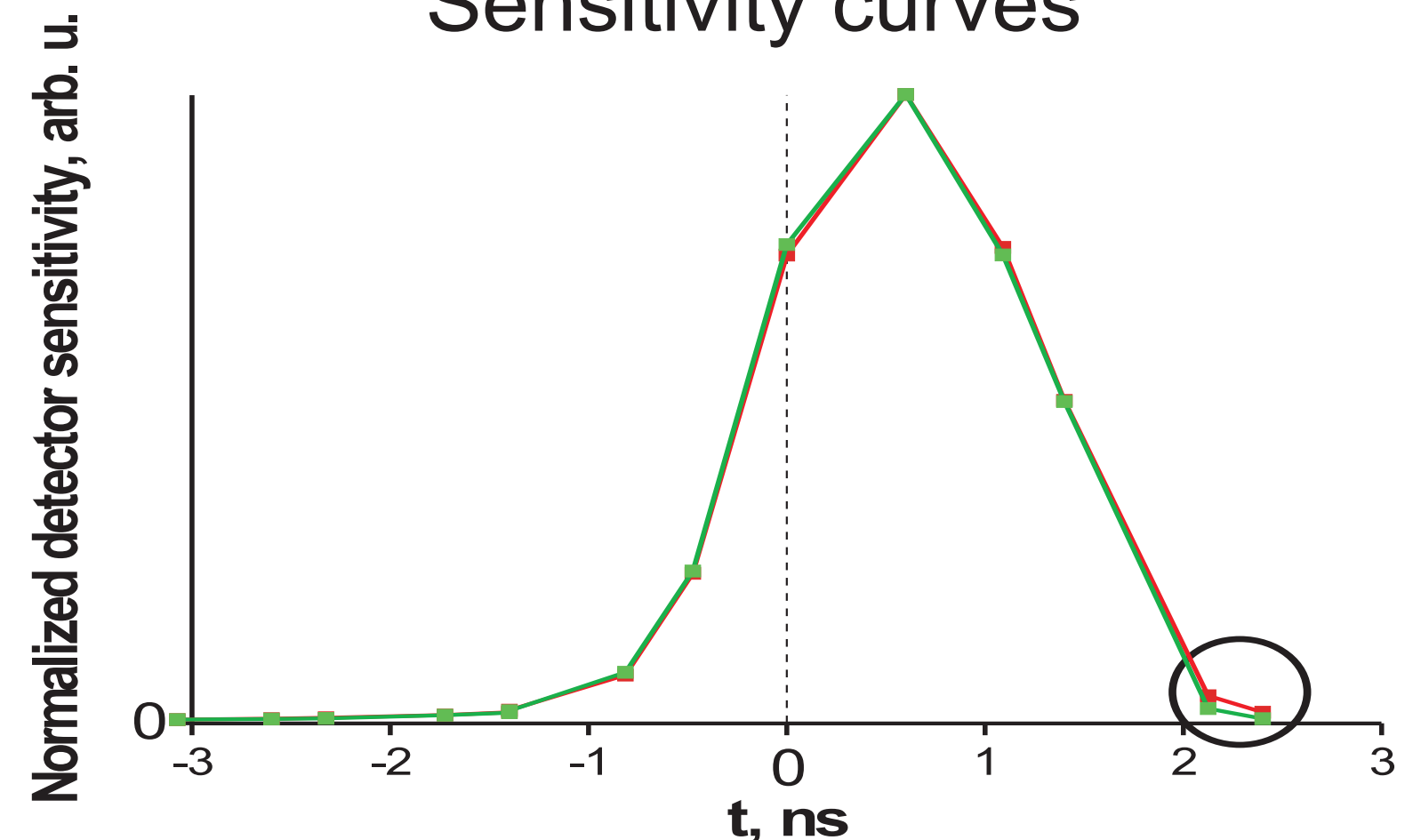
where

$$\eta = \min \left\{ \min_t \frac{\eta_1(t)}{\eta_0(t)}, \min_t \frac{\eta_0(t)}{\eta_1(t)} \right\}$$

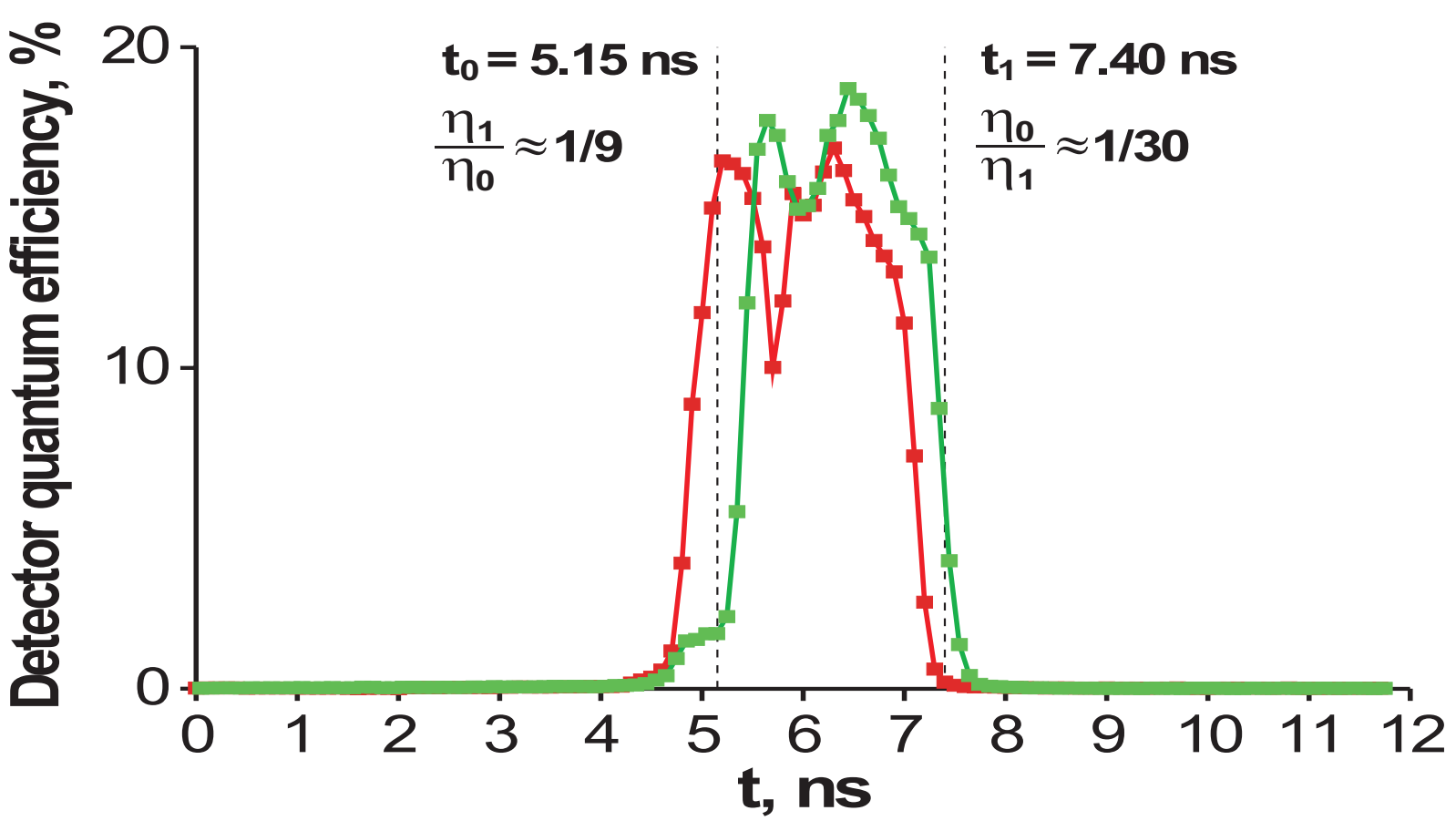
Security state of QKD system



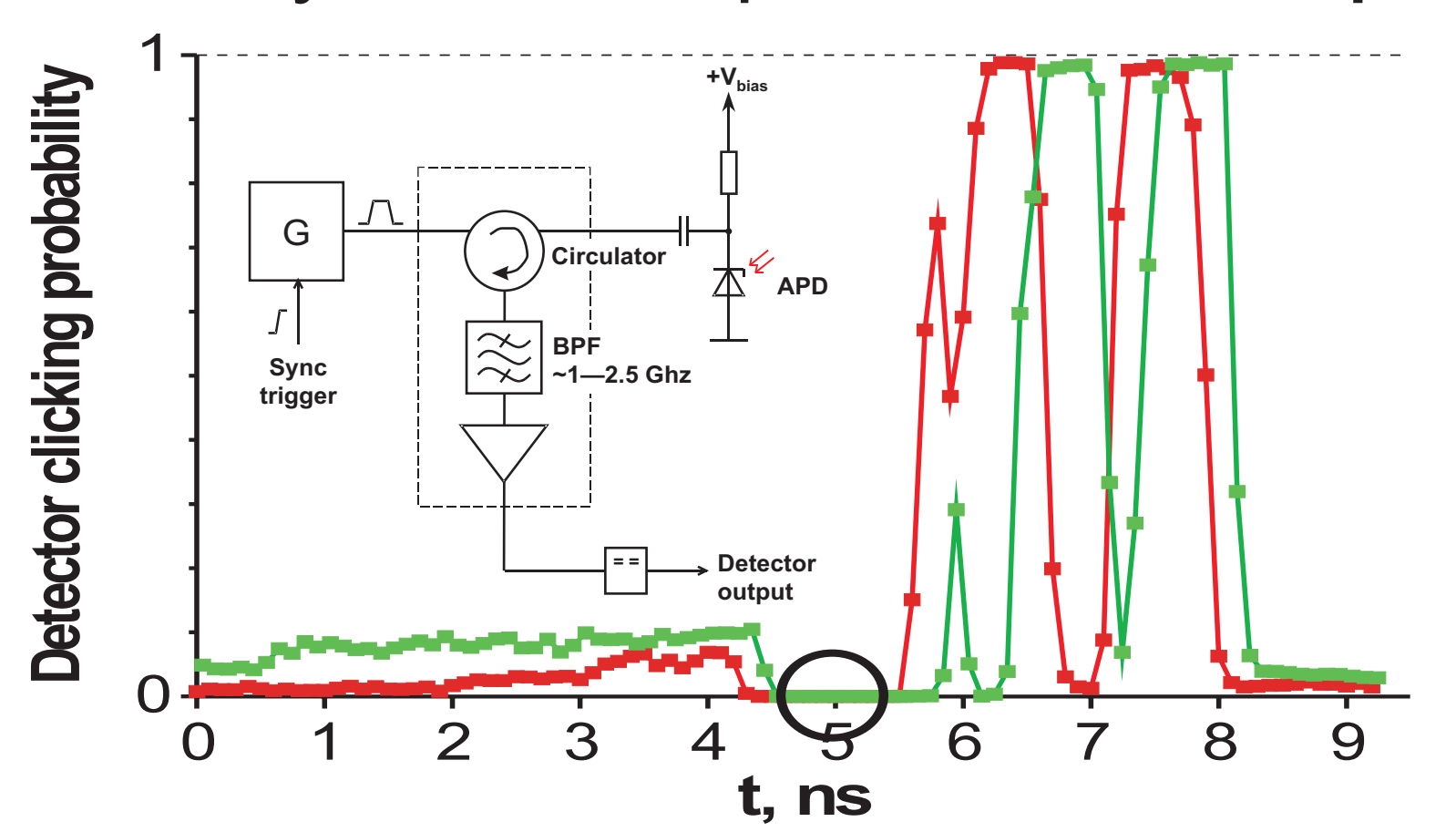
Detector model 1. Sensitivity curves



Detector model 2. Sensitivity curves at low photon number μ=0.5



Sensitivity curves at photon number μ=500

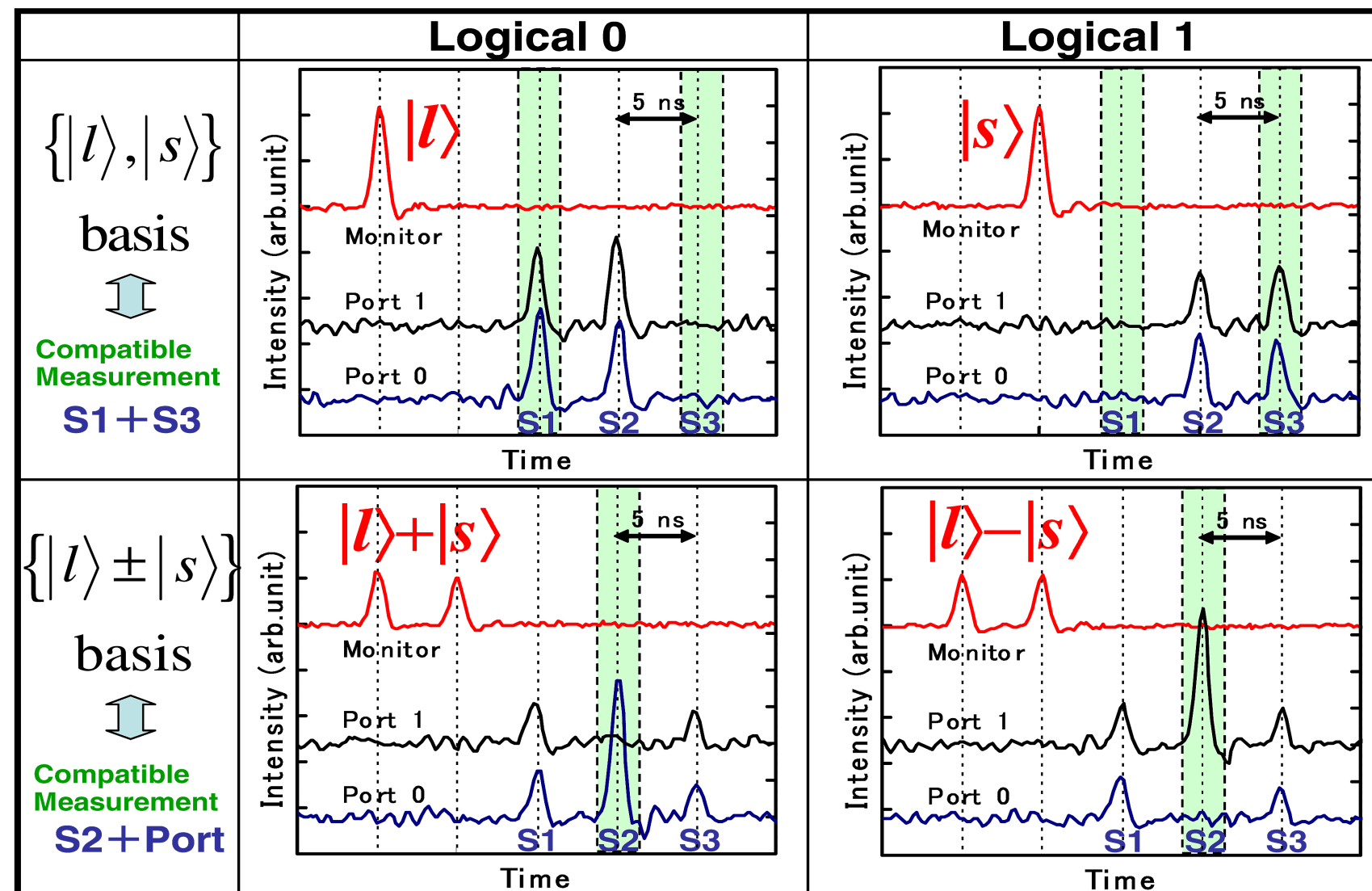
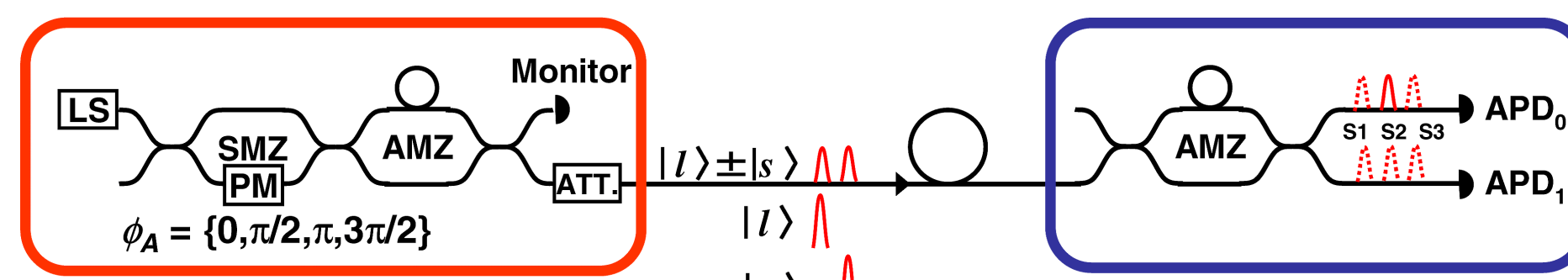


quant-ph/0511032

New results

Phase-time coding

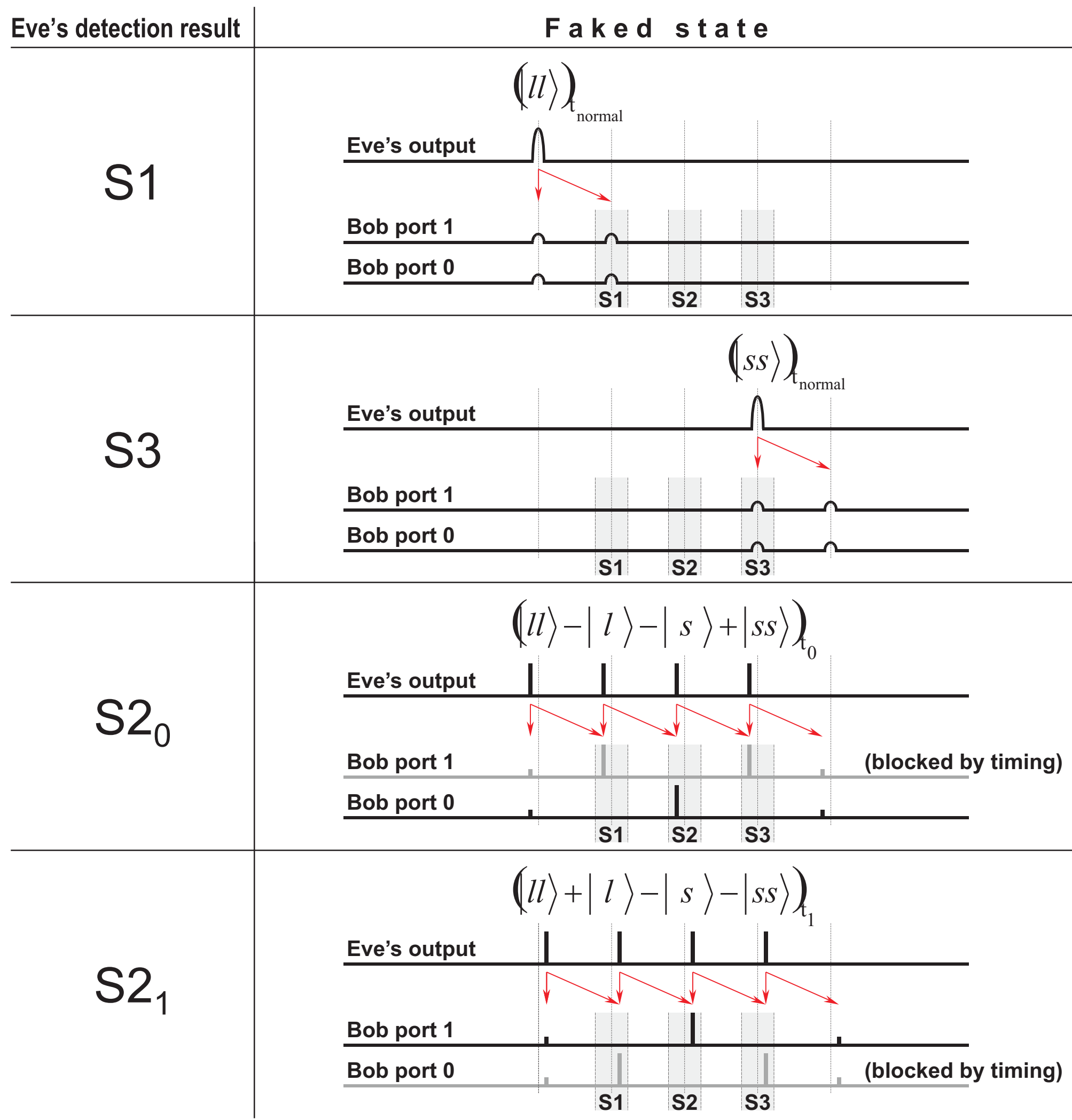
[Y. Nambu, T. Hatanaka, and K. Nakamura, "BB84 quantum key distribution system based on silica-based planar lightwave circuits," Jap. J. Appl. Phys. 43, L1109–L1110 (2004)]



Also used in [W. Tittel, J. Brendel, H. Zbinden, and N. Gisin, "Quantum cryptography using entangled photons in energy-time Bell states," Phys. Rev. Lett. 84, 4737–4740 (2000)]

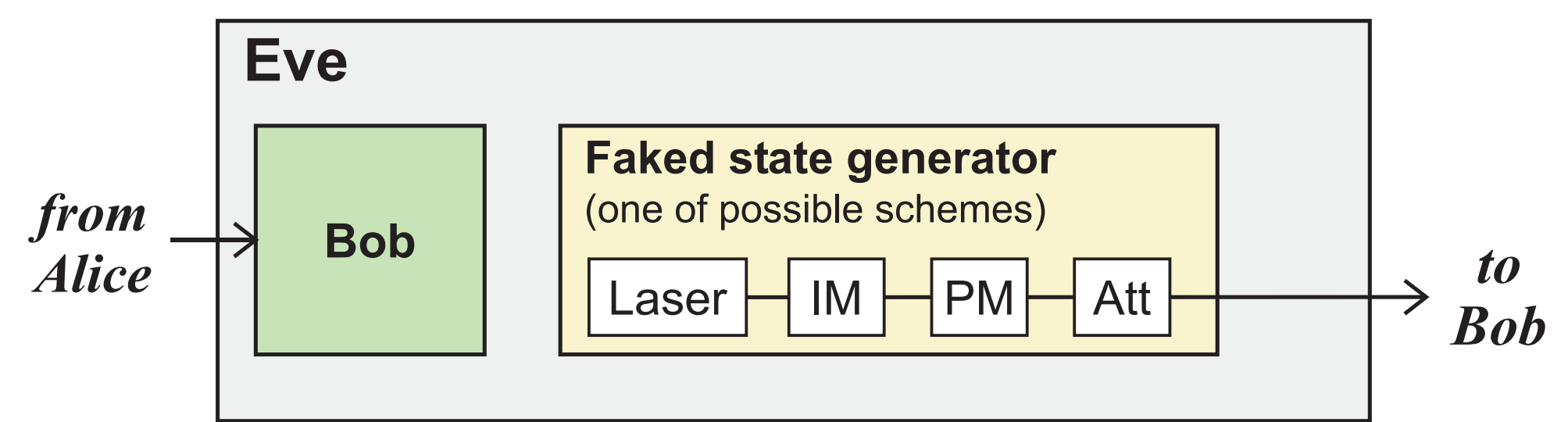
Faked states

(assume use of gated detectors, total efficiency mismatch)



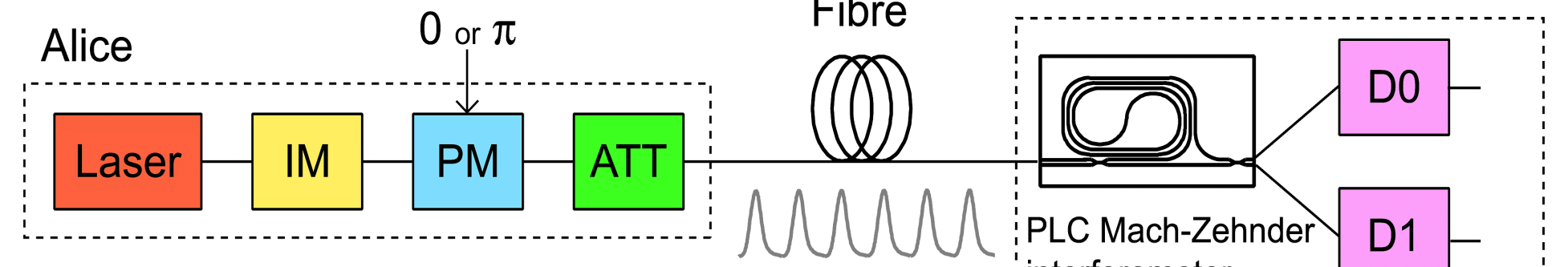
Note that in the case of *partial* efficiency mismatch, only Eve's faked states for S2₀ and S2₁ contribute to QBER. The faked states for S1 and S3 remain error-free.

Eve's setup



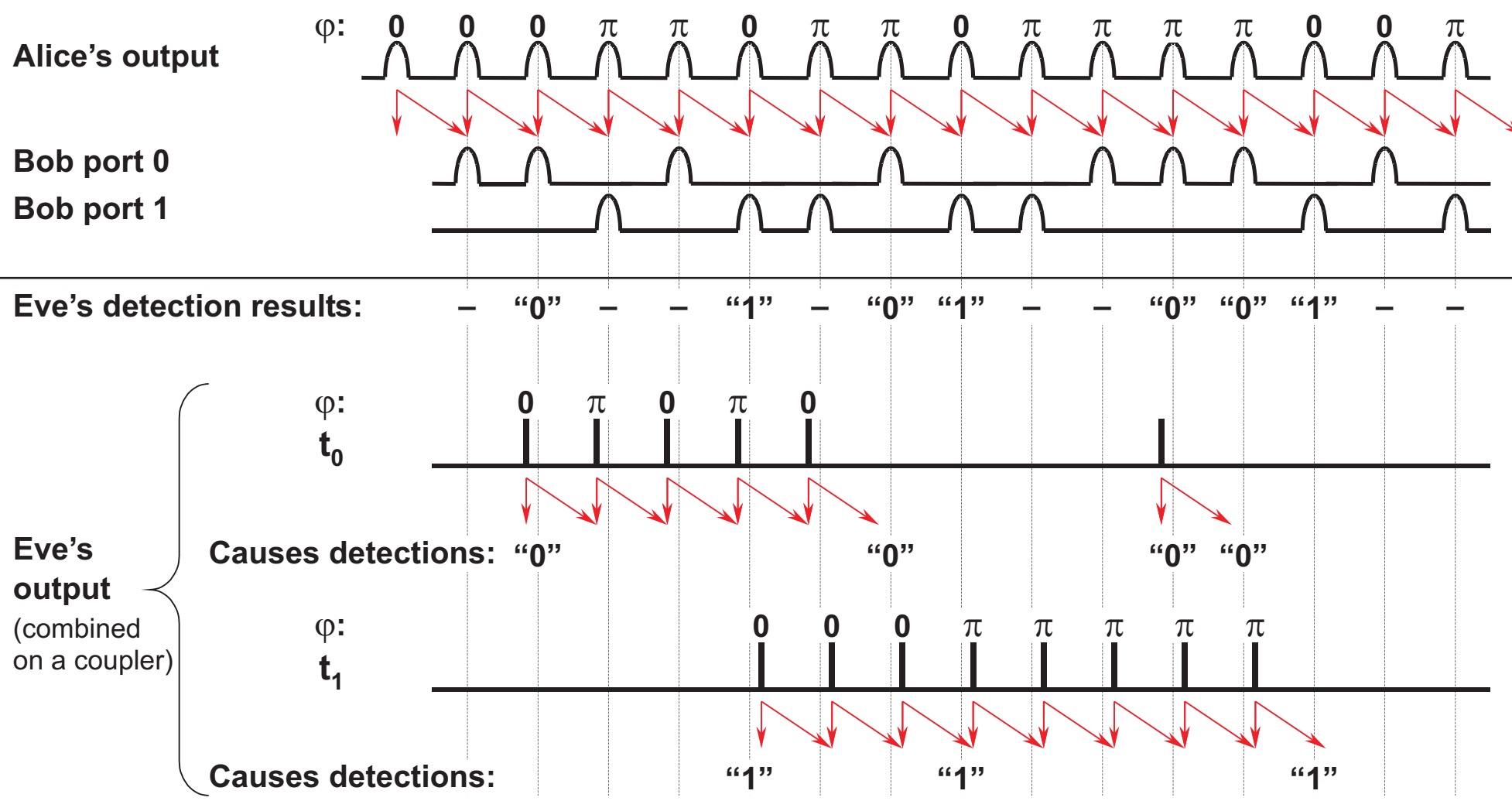
DPSK

[H. Takesue, E. Diamanti, T. Honjo, C. Langrock, M.M. Fejer, K. Inoue, and Y. Yamamoto, "Differential phase shift quantum key distribution experiment over 105 km fibre," New J. Phys. 7, 232 (2005)]

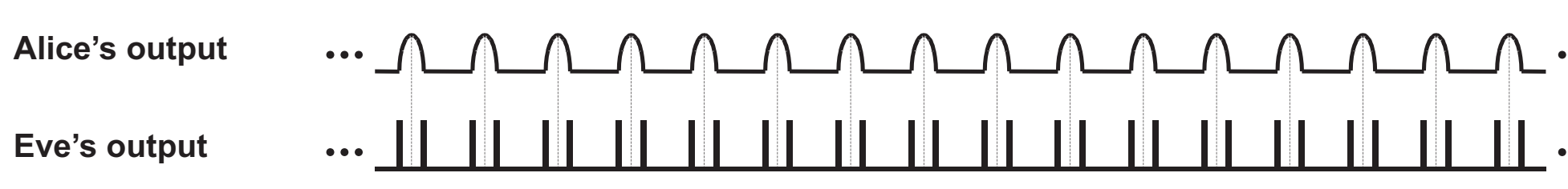


Long, overlapping faked states

(assume total efficiency mismatch)



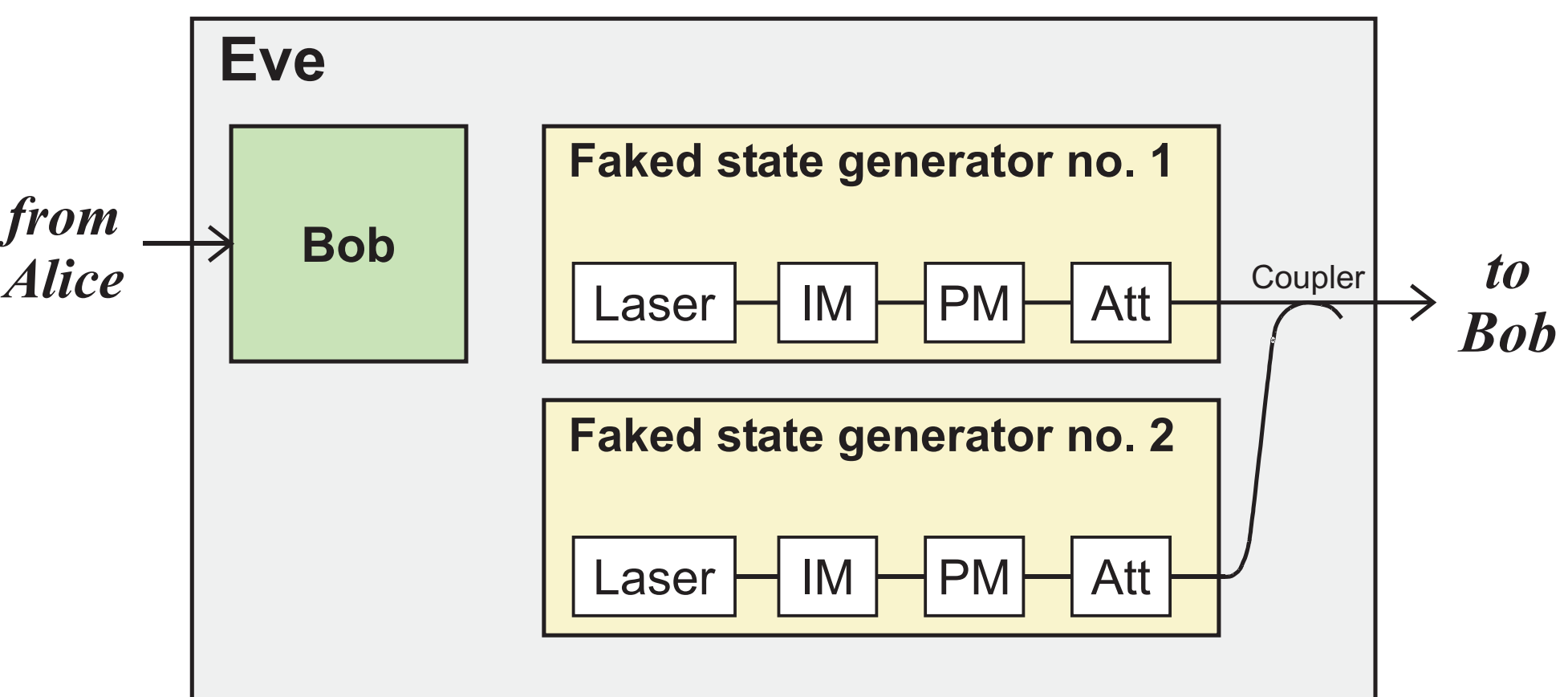
in limit: two continuous trains of pulses from Eve



(We don't know yet if conditions exist under which such a continuous faked state is advantageous in the case of partial efficiency mismatch.)

NB! In this DPSK scheme, the control parameter t Eve uses to select Bob's detector may not be necessarily time, but e.g. wavelength (might be useful with upconversion detectors).

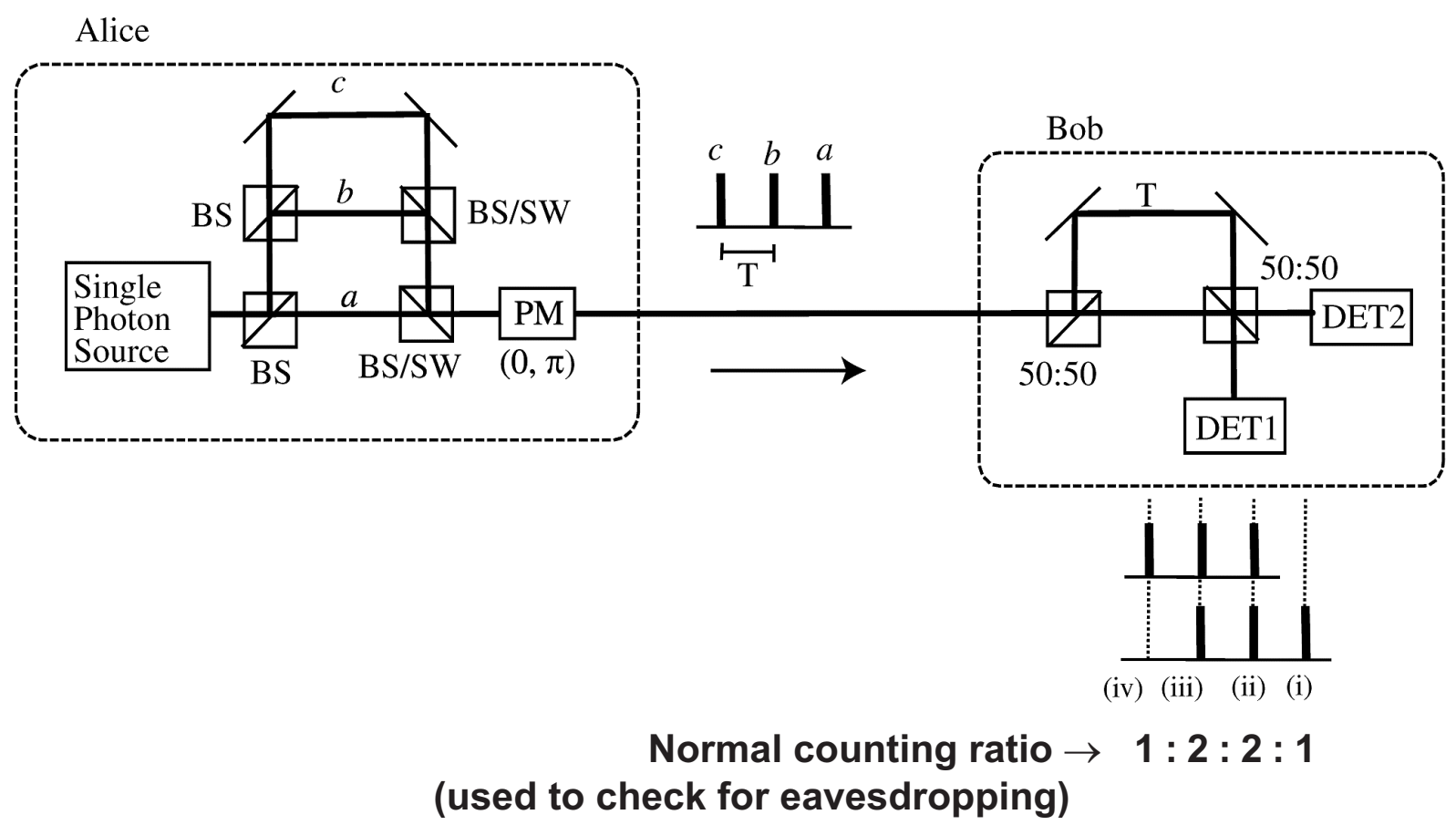
Eve's setup



DPSK with limited-length states

can be eavesdropped on using the methods considered above

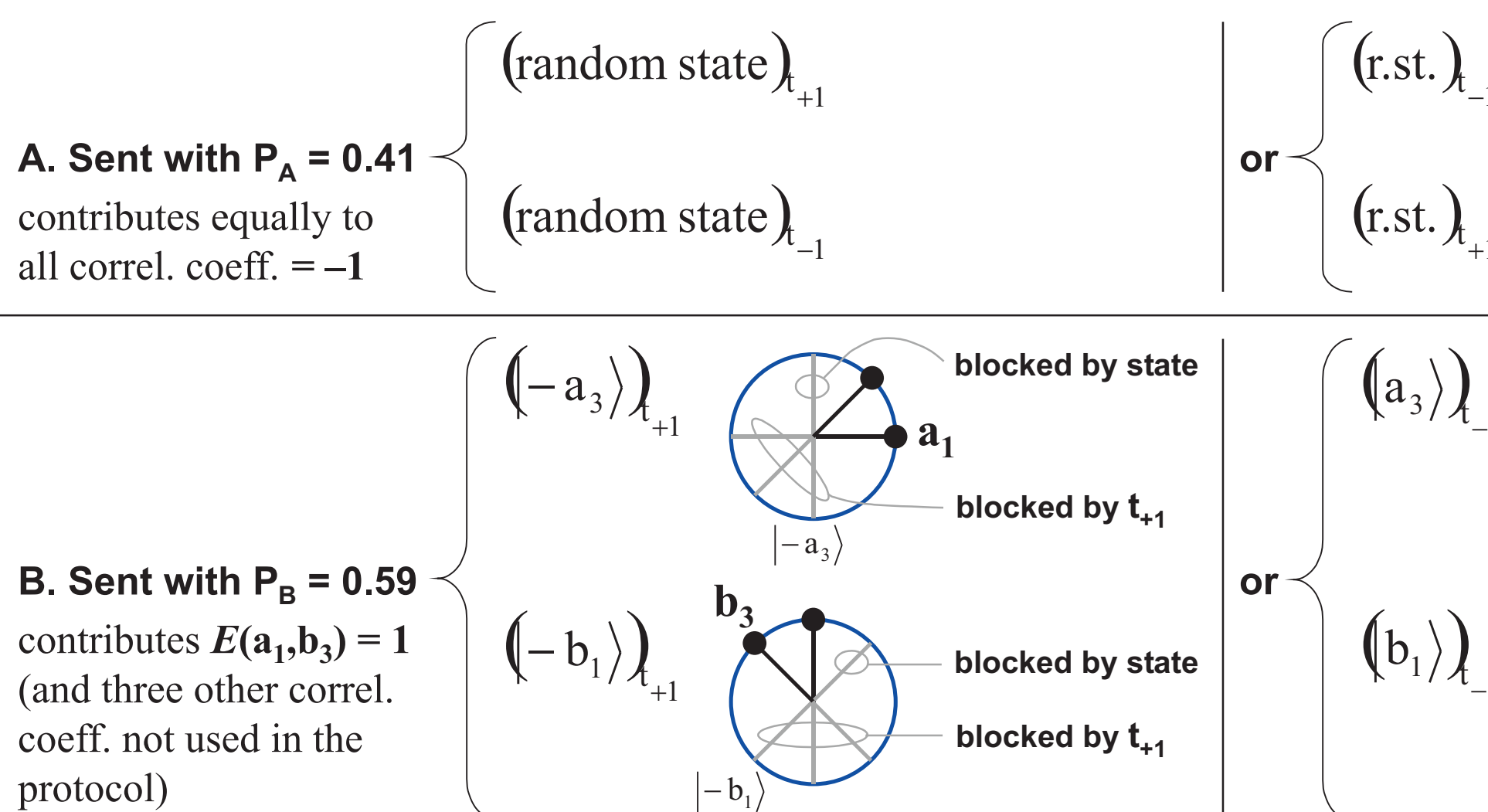
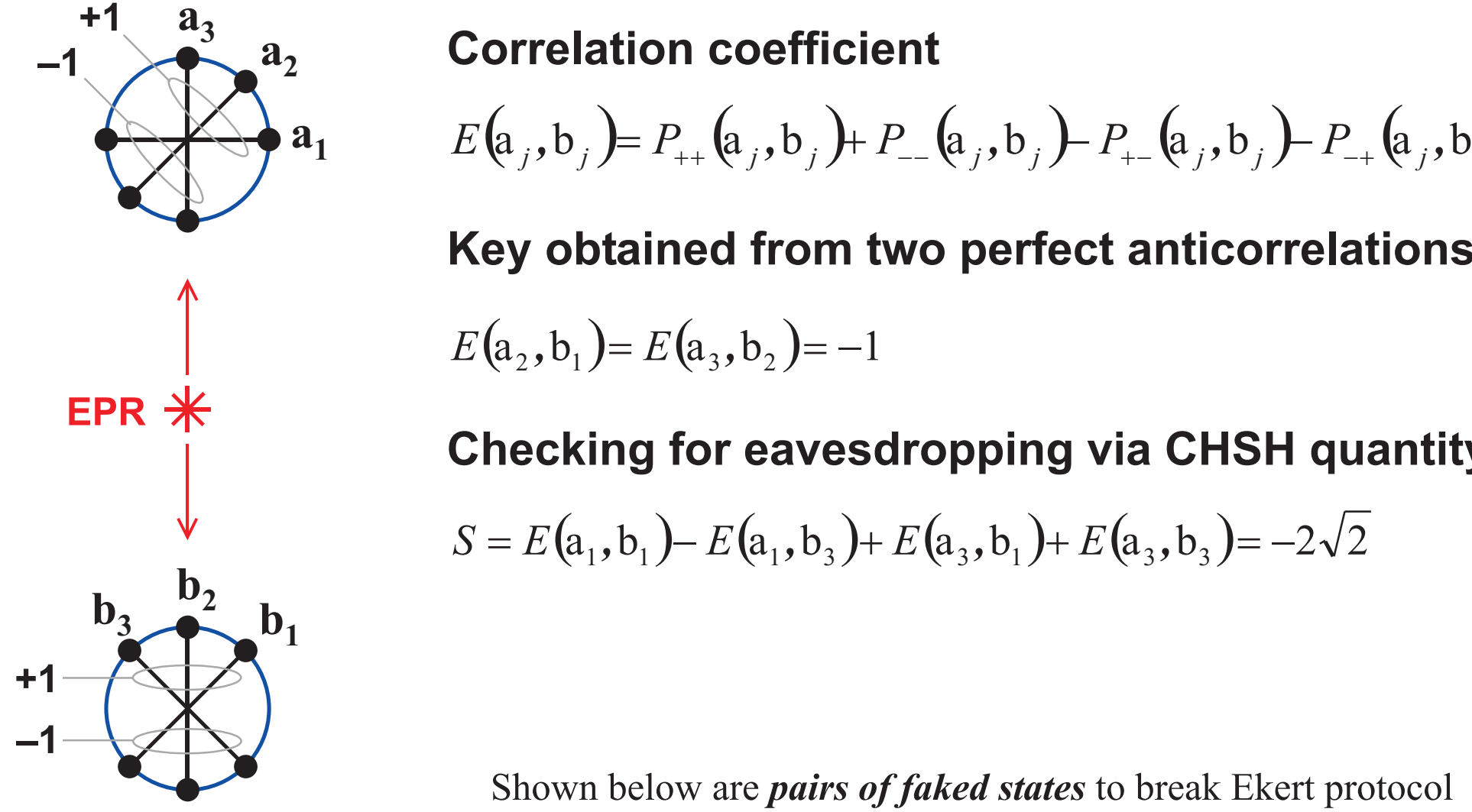
[K. Inoue, E. Waks, and Y. Yamamoto, "Differential phase shift quantum key distribution," Phys. Rev. Lett. 89, 037902 (2002)]



Yet longer states in [W. Buttler, J. Torgerson, and S. Lamoreaux, "New, efficient and robust, fiber-based quantum key distribution schemes," Phys. Lett. A 299, 38–42 (2002)]

Ekert protocol

[A. Ekert, "Quantum cryptography based on Bell's theorem," Phys. Rev. Lett. 67, 661–663 (1991)]



If only A is sent, $S = -1 + 1 - 1 - 1 = -2$

If A and B are sent, $S = -1 + (-2\sqrt{2}) - 1 - 1 = -2\sqrt{2}$

Conclusion

- Detector efficiency mismatch is a problem in many protocols and encodings: BB84, phase-time, DPSK; also in implementations with source of entangled pairs placed outside Alice and Bob (e.g. Ekert protocol).
- The worst-case mismatch must be characterized and accounted for during privacy amplification.
- Active protection measures are possible (monitoring of incoming pulses at Bob).